Package 'projpred'

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Description Performs projection predictive feature selection for generalized linear models (Piironen, Paasiniemi, and Vehtari, 2020, <doi:10.1214/20-EJS1711>) with or without multilevel or additive terms (Catalina, Bürkner, and Vehtari, 2022, <https://proceedings.mlr.press/v151/catalina22a.html>), for some ordinal and nominal regression models (Weber, Glass, and Vehtari, 2025, <doi:10.1007/s00180-024-01506-0>), and for many other regression models (using the latent projection by Catalina, Bürkner, and Vehtari, 2021, <doi:10.48550/arXiv.2109.04702>, which can also be applied to most of the former models). The package is compatible with the 'rstanarm' and 'brms' packages, but other reference models can also be used. See the vignettes and the documentation for more information and examples.

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URL https://mc-stan.org/projpred/, https://discourse.mc-stan.org

BugReports https://github.com/stan-dev/projpred/issues/

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Author Juho Piironen [aut],
Markus Paasiniemi [aut],
Alejandro Catalina [aut],
Frank Weber [aut],
Osvaldo Martin [cre, aut],
Aki Vehtari [aut],
Jonah Gabry [ctb],
Marco Colombo [ctb],
Paul-Christian Bürkner [ctb],
Hamada S. Badr [ctb],
Brian Sullivan [ctb],
Sölvi Rögnvaldsson [ctb],
The LME4 Authors [cph] (see file 'LICENSE' for details),
Yann McLatchie [ctb],
Juho Timonen [ctb]

Maintainer Osvaldo Martin <aloctavodia@gmail.com>

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`projpred-package` *Projection predictive feature selection*

Description

The R package **projpred** performs the projection predictive variable (or "feature") selection for various regression models. We recommend to read the `README` file (available with enhanced formatting online) and the main vignette (`topic = "projpred"`, but also available online) before continuing here.

Terminology

Throughout the whole package documentation, we use the term "submodel" for all kinds of candidate models onto which the reference model is projected. For custom reference models, the candidate models don't need to be actual *sub*models of the reference model, but in any case (even for custom reference models), the candidate models are always actual *sub*models of the full `formula` used by the search procedure. In this regard, it is correct to speak of *sub*models, even in case of a custom reference model.

The following model type abbreviations will be used at multiple places throughout the documentation: GLM (generalized linear model), GLMM (generalized linear multilevel—or "mixed"—model), GAM (generalized additive model), and GAMM (generalized additive multilevel—or "mixed"—model). Note that the term "generalized" includes the Gaussian family as well.

Draw-wise divergence minimizers

For the projection of the reference model onto a submodel, **projpred** currently relies on the following functions as draw-wise divergence minimizers (in other words, these are the workhorse functions employed by **projpred**'s internal default `div_minimizer` functions, see `init_refmodel()`):

- Submodel without multilevel or additive terms:

  - For the traditional (or latent) projection (or the augmented-data projection in case of the `binomial()` or `brms::bernoulli()` family): An internal C++ function which basically serves the same purpose as `lm()` for the `gaussian()` family and `glm()` for all other families. The returned object inherits from class `subfit`. Possible tuning parameters for this internal C++ function are: `regul` (amount of ridge regularization; default: `1e-4`), `thresh_conv` (convergence threshold; default: `1e-7`), `qa_updates_max` (maximum number of quadratic approximation updates; default: `100`, but fixed to `1` in case of the Gaussian family with identity link), `ls_iter_max` (maximum number of line search iterations; default: `30`, but fixed to `1` in case of the Gaussian family with identity link), `normalize` (single logical value indicating whether to scale the predictors internally with the returned regression coefficient estimates being back-adjusted appropriately; default: `TRUE`), `beta0_init` (single numeric value giving the starting value for the intercept at centered predictors; default: `0`), and `beta_init` (numeric vector giving the starting values for the regression coefficients; default: vector of `0`s).
  - For the augmented-data projection: `MASS::polr()` (the returned object inherits from class `polr`) for the `brms::cumulative()` family or `rstanarm::stan_polr()` fits, `nnet::multinom()` (the returned object inherits from class `multinom`) for the `brms::categorical()` family.
- Submodel with multilevel but no additive terms:
  - For the traditional (or latent) projection (or the augmented-data projection in case of the `binomial()` or `brms::bernoulli()` family): `lme4::lmer()` (the returned object inherits from class `lmerMod`) for the `gaussian()` family, `lme4::glmer()` (the returned object inherits from class `glmerMod`) for all other families.
  - For the augmented-data projection: `ordinal::clmm()` (the returned object inherits from class `clmm`) for the `brms::cumulative()` family, `mclogit::mblogit()` (the returned object inherits from class `mmblogit`) for the `brms::categorical()` family.
- Submodel without multilevel but additive terms: `mgcv::gam()` (the returned object inherits from class `gam`).
- Submodel with multilevel and additive terms: `gamm4::gamm4()` (within **projpred**, the returned object inherits from class `gamm4`).

Verbosity, messages, warnings, errors

Global option `projpred.verbose` may be used for specifying the value passed to argument `verbose` of `project()`, `varsel()`, and `cv_varsel()`.

By default, **projpred** catches messages and warnings from the draw-wise divergence minimizers and throws their unique collection after performing all draw-wise divergence minimizations (i.e., draw-wise projections). This can be deactivated by setting global option `projpred.warn_proj_drawwise` to `FALSE`.

Furthermore, by default, **projpred** checks the convergence of the draw-wise divergence minimizers and throws a warning if any seem to have not converged. This warning is thrown after the warning message from global option `projpred.warn_proj_drawwise` (see above) and can be deactivated by setting global option `projpred.check_convergence` to `FALSE`.

Parallelization

The projection of the reference model onto a submodel can be run in parallel (across the projected draws). This is powered by the **foreach** package. Thus, any parallel (or sequential) backend compatible with **foreach** can be used, e.g., the backends from packages **doParallel**, **doMPI**, or **doFuture**.

Using the global option `projpred.parallel_proj_trigger`, the number of projected draws below which no parallelization is applied (even if a parallel backend is registered) can be modified. Such a "trigger" threshold exists because of the computational overhead of a parallelization which makes the projection parallelization only useful for a sufficiently large number of projected draws. By default, the projection parallelization is turned off, which can also be achieved by supplying `Inf` (or `NULL`) to option `projpred.parallel_proj_trigger`. Note that we cannot recommend the projection parallelization on Windows because in our experience, the parallelization overhead is larger there, causing a parallel run to take longer than a sequential run. Also note that the projection parallelization works well for submodels which are GLMs (and hence also for the latent projection if the submodel has no multilevel or additive predictor terms), but for all other types of submodels, the fitted submodel objects are quite big, which—when running in parallel—may lead to excessive memory usage which in turn may crash the R session (on Unix systems, setting an appropriate memory limit via `unix::rlimit_as()` may avoid crashing the whole machine). Thus, we currently cannot recommend parallelizing projections onto submodels which are GLMs (in this context, the latent projection onto a submodel without multilevel and without additive terms may be regarded as a projection onto a submodel which is a GLM). However, for `cv_varsel()`, there is also a *CV* parallelization (i.e., a parallelization of **projpred**'s cross-validation) which can be activated via argument `parallel` (which in turn can be controlled via global option `projpred.parallel_cv`).

For the CV parallelization, global option `projpred.export_to_workers` may be set to a character vector of names of objects to export from the global environment to the parallel workers.

During parallelization (either of the projection or the CV), progression updates can be received via the **progressr** package. This only works if the **doFuture** backend is used for parallelization, e.g., via `doFuture::registerDoFuture()` and `future::plan(future::multisession, workers = 4)`. In that case, the **progressr** package can be used, e.g., by calling `progressr::handlers(global = TRUE)` before running the projection or the CV in parallel. The **projpred** package also offers the global option `projpred.use_progressr` for controlling whether to use the **progressr** package (`TRUE` or `FALSE`), but since that global option defaults to `requireNamespace("progressr", quietly = TRUE) && interactive() && identical(foreach::getDoParName(), "doFuture")`, it usually does not need to be set by the user.

Multilevel models: "Integrating out" group-level effects

In case of multilevel models, **projpred** offers two global options for "integrating out" group-level effects: `projpred.mlvl_pred_new` and `projpred.mlvl_proj_ref_new`. When setting `projpred.mlvl_pred_new` to `TRUE` (default is `FALSE`), then at *prediction* time, **projpred** will treat group levels existing in the training data as *new* group levels, implying that their group-level effects are drawn randomly from a (multivariate) Gaussian distribution. This concerns both, the reference model and the (i.e., any) submodel. Furthermore, setting `projpred.mlvl_pred_new` to `TRUE` causes `as.matrix.projection()` and `as_draws_matrix.projection()` to omit the projected group-level effects (for the group levels from the original dataset). When setting `projpred.mlvl_proj_ref_new` to `TRUE` (default is `FALSE`), then at *projection* time, the reference model's fitted values (that the submodels fit to) will be computed by treating the group levels from the original dataset as *new* group levels, implying that their group-level effects will be drawn randomly from a (multivariate) Gaussian distribution (as long as the reference model is a multilevel model, which—for custom reference models—does not need to be the case). This also affects the latent response values for a latent projection correspondingly. Setting `projpred.mlvl_pred_new` to `TRUE` makes sense, e.g., when the prediction task is such that any group level will be treated as a new one. Typically, setting `projpred.mlvl_proj_ref_new` to `TRUE` only makes sense when `projpred.mlvl_pred_new` is already set to `TRUE`. In that case, the de-

fault of FALSE for projpred.mlvl_proj_ref_new ensures that at projection time, the submodels fit to the best possible fitted values from the reference model, and setting projpred.mlvl_proj_ref_new to TRUE would make sense if the group-level effects should be integrated out completely.

Memory usage

By setting the global option projpred.run_gc to TRUE, **projpred** will call gc() at some places (e.g., after each size that the forward search passes through) to free up some memory. These gc() calls are not always necessary to reduce the peak memory usage, but they add runtime (hence the default of FALSE for that global option).

Other notes

Global option projpred.digits controls arguments digits of print.vselsummary() and print.vsel().

There are several global options to control arguments of plot.vsel() and plot.cv_proportions() globally, see section "Usage" of the help pages of these two functions.

Global option projpred.warn_L1_interactions may be set to FALSE to deactivate a warning that an L1 search selected an interaction term before all involved lower-order interaction terms (including main-effect terms) were selected (in which case the predictor ranking is automatically modified by **projpred** so that the lower-order interaction terms come before this interaction term).

Most examples are not executed when called via example(). To execute them, their code has to be copied and pasted manually to the console.

Functions

init_refmodel(), get_refmodel() For setting up an object containing information about the reference model, the submodels, and how the projection should be carried out. Explicit calls to init_refmodel() and get_refmodel() are only rarely needed.

varsel(), cv_varsel() For running the *search* part and the *evaluation* part for a projection predictive variable selection, possibly with cross-validation (CV).

summary.vsel(), print.vsel(), plot.vsel(), suggest_size.vsel(), ranking(), cv_proportions(), plot.cv_prop
For post-processing the results from varsel() and cv_varsel().

project() For projecting the reference model onto submodel(s). Typically, this follows the variable selection, but it can also be applied directly (without a variable selection).

as.matrix.projection() **and** as_draws_matrix.projection() For extracting projected parameter draws.

proj_linpred(), proj_predict() For making predictions from a submodel (after projecting the reference model onto it).

Author(s)

Maintainer: Osvaldo Martin <aloctavodia@gmail.com>

Authors:

- Osvaldo Martin <aloctavodia@gmail.com>
- Juho Piironen <juho.t.piironen@gmail.com>

- Markus Paasiniemi
- Alejandro Catalina <alecatfel@gmail.com>
- Frank Weber
- Aki Vehtari

Other contributors:

- Jonah Gabry [contributor]
- Marco Colombo [contributor]
- Paul-Christian Bürkner [contributor]
- Hamada S. Badr [contributor]
- Brian Sullivan [contributor]
- Sölvi Rögnvaldsson [contributor]
- The LME4 Authors (see file 'LICENSE' for details) [copyright holder]
- Yann McLatchie [contributor]
- Juho Timonen [contributor]

See Also

Useful links:

- https://mc-stan.org/projpred/
- https://discourse.mc-stan.org
- Report bugs at https://github.com/stan-dev/projpred/issues/

`as.matrix.projection` *Extract projected parameter draws and coerce to matrix*

Description

This is the `as.matrix()` method for `projection` objects (returned by `project()`, possibly as elements of a `list`). It extracts the projected parameter draws and returns them as a matrix. In case of different (i.e., nonconstant) weights for the projected draws, see `as_draws_matrix.projection()` for a better solution.

Usage

```
## S3 method for class 'projection'
as.matrix(x, nm_scheme = NULL, allow_nonconst_wdraws_prj = FALSE, ...)
```

Arguments

x	An object of class `projection` (returned by `project()`, possibly as elements of a `list`).
nm_scheme	The naming scheme for the columns of the output matrix. Either `NULL`, `"rstanarm"`, or `"brms"`, where `NULL` chooses `"rstanarm"` or `"brms"` based on the class of the reference model fit (and uses `"rstanarm"` if the reference model fit is of an unknown class).
allow_nonconst_wdraws_prj	A single logical value indicating whether to allow projected draws with different (i.e., nonconstant) weights (`TRUE`) or not (`FALSE`). **CAUTION**: Expert use only because if set to `TRUE`, the weights of the projected draws are stored in an attribute `wdraws_prj` and handling this attribute requires special care (e.g., when subsetting the returned matrix).
...	Currently ignored.

Details

In case of the augmented-data projection for a multilevel submodel of a `brms::categorical()` reference model, the multilevel parameters (and therefore also their names) slightly differ from those in the **brms** reference model fit (see section "Augmented-data projection" in `extend_family()`'s documentation).

Value

An $S_{\text{prj}} \times Q$ matrix of projected draws, with S_{prj} denoting the number of projected draws and Q the number of parameters. If `allow_nonconst_wdraws_prj` is set to `TRUE`, the weights of the projected draws are stored in an attribute `wdraws_prj`. (If `allow_nonconst_wdraws_prj` is `FALSE`, projected draws with nonconstant weights cause an error.)

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Projection onto an arbitrary combination of predictor terms (with a small
# value for `ndraws`, but only for the sake of speed in this example; this
# is not recommended in general):
prj <- project(fit, predictor_terms = c("X1", "X3", "X5"), ndraws = 21,
               seed = 9182)

# Applying the as.matrix() generic to the output of project() dispatches to
```

```
# the projpred::as.matrix.projection() method:
prj_mat <- as.matrix(prj)

# Since the draws have all the same weight here, we can treat them like
# ordinary MCMC draws, e.g., we can summarize them using the `posterior`
# package:
if (requireNamespace("posterior", quietly = TRUE)) {
  print(posterior::summarize_draws(
    posterior::as_draws_matrix(prj_mat),
    "median", "mad", function(x) quantile(x, probs = c(0.025, 0.975))
  ))
}
# Or visualize them using the `bayesplot` package:
if (requireNamespace("bayesplot", quietly = TRUE)) {
  print(bayesplot::mcmc_intervals(prj_mat))
}
```

`as_draws_matrix.projection` *Extract projected parameter draws and coerce to* `draws_matrix` *(see package* **posterior***)*

Description

These are the `posterior::as_draws()` and `posterior::as_draws_matrix()` methods for `projection` objects (returned by `project()`, possibly as elements of a `list`). They extract the projected parameter draws and return them as a `draws_matrix`. In case of different (i.e., nonconstant) weights for the projected draws, a `draws_matrix` allows for a safer handling of these weights (safer in contrast to the matrix returned by `as.matrix.projection()`), in particular by providing the natural input for `posterior::resample_draws()` (see section "Examples" below).

Usage

```
## S3 method for class 'projection'
as_draws_matrix(x, ...)

## S3 method for class 'projection'
as_draws(x, ...)
```

Arguments

`x`	An object of class `projection` (returned by `project()`, possibly as elements of a `list`).
`...`	Arguments passed to `as.matrix.projection()`, except for `allow_nonconst_wdraws_prj`.

Details

In case of the augmented-data projection for a multilevel submodel of a `brms::categorical()` reference model, the multilevel parameters (and therefore also their names) slightly differ from those in the **brms** reference model fit (see section "Augmented-data projection" in `extend_family()`'s documentation).

Value

An $S_{\text{prj}} \times Q$ `draws_matrix` (see `posterior::draws_matrix()`) of projected draws, with S_{prj} denoting the number of projected draws and Q the number of parameters. If the projected draws have nonconstant weights, `posterior::weight_draws()` is applied internally.

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Projection onto an arbitrary combination of predictor terms (with a small
# value for `nclusters`, but only for illustrative purposes; this is not
# recommended in general):
prj <- project(fit, predictor_terms = c("X1", "X3", "X5"), nclusters = 5,
               seed = 9182)

# Applying the posterior::as_draws_matrix() generic to the output of
# project() dispatches to the projpred::as_draws_matrix.projection()
# method:
prj_draws <- posterior::as_draws_matrix(prj)

# Resample the projected draws according to their weights:
set.seed(3456)
prj_draws_resampled <- posterior::resample_draws(prj_draws, ndraws = 1000)

# The values from the following two objects should be the same (in general,
# this only holds approximately):
print(proportions(table(rownames(prj_draws_resampled))))
print(weights(prj_draws))

# Treat the resampled draws like ordinary draws, e.g., summarize them:
print(posterior::summarize_draws(
  prj_draws_resampled,
  "median", "mad", function(x) quantile(x, probs = c(0.025, 0.975))
))
# Or visualize them using the `bayesplot` package:
```

```
if (requireNamespace("bayesplot", quietly = TRUE)) {
  print(bayesplot::mcmc_intervals(prj_draws_resampled))
}
```

`augdat_ilink_binom` *Inverse-link function for augmented-data projection with binomial family*

Description

This is the function which has to be supplied to `extend_family()`'s argument `augdat_ilink` in case of the augmented-data projection for the `binomial()` family.

Usage

```
augdat_ilink_binom(eta_arr, link = "logit")
```

Arguments

`eta_arr`	An array as described in section "Augmented-data projection" of `extend_family()`'s documentation.
`link`	The same as argument `link` of `binomial()`.

Value

An array as described in section "Augmented-data projection" of `extend_family()`'s documentation.

`augdat_link_binom` *Link function for augmented-data projection with binomial family*

Description

This is the function which has to be supplied to `extend_family()`'s argument `augdat_link` in case of the augmented-data projection for the `binomial()` family.

Usage

```
augdat_link_binom(prb_arr, link = "logit")
```

Arguments

`prb_arr`	An array as described in section "Augmented-data projection" of `extend_family()`'s documentation.
`link`	The same as argument `link` of `binomial()`.

Value

An array as described in section "Augmented-data projection" of `extend_family()`'s documentation.

`break_up_matrix_term` *Break up matrix terms*

Description

Sometimes there can be terms in a formula that refer to a matrix instead of a single predictor. This function breaks up the matrix term into individual predictors to handle separately, as that is probably the intention of the user.

Usage

```
break_up_matrix_term(formula, data)
```

Arguments

`formula`	A `formula` for a valid model.
`data`	The original `data.frame` with a matrix as predictor.

Value

A `list` containing the expanded `formula` and the expanded `data.frame`.

`cl_agg` *Weighted averaging within clusters of parameter draws*

Description

This function aggregates S parameter draws that have been clustered into S_{cl} clusters by averaging across the draws that belong to the same cluster. This averaging can be done in a weighted fashion.

Usage

```
cl_agg(
  draws,
  cl = seq_len(nrow(draws)),
  wdraws = rep(1, nrow(draws)),
  eps_wdraws = 0
)
```

Arguments

draws	An $S \times P$ matrix of parameter draws, with P denoting the number of parameters.
cl	A numeric vector of length S, giving the cluster indices for the draws. The cluster indices need to be values from the set $\{1, ..., S_{\text{cl}}\}$, except for draws that should be dropped (e.g., by thinning), in which case NA needs to be provided at the positions of cl corresponding to these draws.
wdraws	A numeric vector of length S, giving the weights of the draws. It doesn't matter whether these are normalized (i.e., sum to 1) or not because internally, these weights are normalized to sum to 1 within each cluster. Draws that should be dropped (e.g., by thinning) can (but must not necessarily) have an NA in wdraws.
eps_wdraws	A positive numeric value (typically small) which will be used to improve numerical stability: The weights of the draws within each cluster are multiplied by 1 - eps_wdraws. The default of 0 should be fine for most cases; this argument only exists to help in those cases where numerical instabilities occur (which must be detected by the user; this function will not detect numerical instabilities itself).

Value

An $S_{\text{cl}} \times P$ matrix of aggregated parameter draws.

Examples

```
set.seed(323)
S <- 100L
P <- 3L
draws <- matrix(rnorm(S * P), nrow = S, ncol = P)
# Clustering example:
S_cl <- 10L
cl_draws <- sample.int(S_cl, size = S, replace = TRUE)
draws_cl <- cl_agg(draws, cl = cl_draws)
# Clustering example with nonconstant `wdraws`:
w_draws <- rgamma(S, shape = 4)
draws_cl <- cl_agg(draws, cl = cl_draws, wdraws = w_draws)
# Thinning example (implying constant `wdraws`):
S_th <- 50L
idxs_thin <- round(seq(1, S, length.out = S_th))
th_draws <- rep(NA, S)
th_draws[idxs_thin] <- seq_len(S_th)
draws_th <- cl_agg(draws, cl = th_draws)
```

---

cv-indices *Create cross-validation folds*

Description

These are helper functions to create cross-validation (CV) folds, i.e., to split up the indices from 1 to n into K subsets ("folds") for K-fold CV. These functions are potentially useful when creating the input for arguments cvfits and cvfun of init_refmodel() (or argument cvfits of cv_varsel.refmodel()). Function cvfolds() is deprecated; please use cv_folds() instead (apart from the name, they are the same). The return value of cv_folds() and cv_ids() is different, see below for details.

Usage

```
cv_folds(n, K, seed = NA)

cvfolds(n, K, seed = NA)

cv_ids(n, K, out = c("foldwise", "indices"), seed = NA)
```

Arguments

n	Number of observations.
K	Number of folds. Must be at least 2 and not exceed n.
seed	Pseudorandom number generation (PRNG) seed by which the same results can be obtained again if needed. Passed to argument seed of set.seed(), but can also be NA to not call set.seed() at all. If not NA, then the PRNG state is reset (to the state before calling cv_folds() or cv_ids()) upon exiting cv_folds() or cv_ids().
out	Format of the output, either "foldwise" or "indices". See below for details.

Value

cv_folds() returns a vector of length n such that each element is an integer between 1 and K denoting which fold the corresponding data point belongs to. The return value of cv_ids() depends on the out argument. If out = "foldwise", the return value is a list with K elements, each being a list with elements tr and ts giving the training and test indices, respectively, for the corresponding fold. If out = "indices", the return value is a list with elements tr and ts each being a list with K elements giving the training and test indices, respectively, for each fold.

Examples

```
n <- 100
set.seed(1234)
y <- rnorm(n)
cv <- cv_ids(n, K = 5)
# Mean within the test set of each fold:
cvmeans <- sapply(cv, function(fold) mean(y[fold$ts]))
```

cv_proportions *Ranking proportions from fold-wise predictor rankings*

Description

Calculates the *ranking proportions* from the fold-wise predictor rankings in a cross-validation (CV) with fold-wise searches. For a given predictor x and a given submodel size j, the ranking proportion is the proportion of CV folds which have predictor x at position j of their predictor ranking. While these ranking proportions are helpful for investigating variability in the predictor ranking, they can also be *cumulated* across submodel sizes. The cumulated ranking proportions are more helpful when it comes to model selection.

Usage

```
cv_proportions(object, ...)

## S3 method for class 'ranking'
cv_proportions(object, cumulate = FALSE, ...)

## S3 method for class 'vsel'
cv_proportions(object, ...)
```

Arguments

object	For cv_proportions.ranking(): an object of class ranking (returned by ranking()). For cv_proportions.vsel(): an object of class vsel (returned by varsel() or cv_varsel()) that ranking() will be applied to internally before then calling cv_proportions.ranking().
...	For cv_proportions.vsel(): arguments passed to ranking.vsel() and cv_proportions.ranking(). For cv_proportions.ranking(): currently ignored.
cumulate	A single logical value indicating whether the ranking proportions should be cumulated across increasing submodel sizes (TRUE) or not (FALSE).

Value

A numeric matrix containing the ranking proportions. This matrix has nterms_max rows and nterms_max columns, with nterms_max as specified in the (possibly implicit) ranking() call. The rows correspond to the submodel sizes and the columns to the predictor terms (sorted according to the full-data predictor ranking). If cumulate is FALSE, then the returned matrix is of class cv_proportions. If cumulate is TRUE, then the returned matrix is of classes cv_proportions_cumul and cv_proportions (in this order).

Note that if cumulate is FALSE, then the values in the returned matrix only need to sum to 1 (column-wise and row-wise) if nterms_max (see above) is equal to the full model size. Likewise, if cumulate is TRUE, then the value 1 only needs to occur in each column of the returned matrix if nterms_max is equal to the full model size.

The cv_proportions() function is only applicable if the ranking object includes fold-wise predictor rankings (i.e., if it is based on a vsel object created by cv_varsel() with validate_search = TRUE). If the ranking object contains only a full-data predictor ranking (i.e., if it is based on a vsel object created by varsel() or by cv_varsel(), but the latter with validate_search = FALSE), then an error is thrown because in that case, there are no fold-wise predictor rankings from which to calculate ranking proportions.

See Also

plot.cv_proportions()

Examples

```
# For an example, see `?plot.cv_proportions`.
```

---

cv_varsel *Run search and performance evaluation with cross-validation*

Description

Run the *search* part and the *evaluation* part for a projection predictive variable selection. The search part determines the predictor ranking (also known as solution path), i.e., the best submodel for each submodel size (number of predictor terms). The evaluation part determines the predictive performance of the submodels along the predictor ranking. In contrast to varsel(), cv_varsel() performs a cross-validation (CV) by running the search part with the training data of each CV fold separately (an exception is explained in section "Note" below) and by running the evaluation part on the corresponding test set of each CV fold. A special method is cv_varsel.vsel() because it re-uses the search results from an earlier cv_varsel() (or varsel()) run, as illustrated in the main vignette.

Usage

```
cv_varsel(object, ...)

## Default S3 method:
cv_varsel(object, ...)

## S3 method for class 'vsel'
cv_varsel(
  object,
  cv_method = object$cv_method %||% "LOO",
  nloo = object$nloo,
  K = object$K %||% if (!inherits(object, "datafit")) 5 else 10,
  cvfits = object$cvfits,
  validate_search = object$validate_search %||% TRUE,
  ...
```

```
)

## S3 method for class 'refmodel'
cv_varsel(
  object,
  method = "forward",
  cv_method = if (!inherits(object, "datafit")) "LOO" else "kfold",
  ndraws = NULL,
  nclusters = 20,
  ndraws_pred = 400,
  nclusters_pred = NULL,
  refit_prj = !inherits(object, "datafit"),
  nterms_max = NULL,
  penalty = NULL,
  verbose = getOption("projpred.verbose", as.integer(interactive())),
  nloo = if (cv_method == "LOO") object$nobs else NULL,
  K = if (!inherits(object, "datafit")) 5 else 10,
  cvfits = object$cvfits,
  search_control = NULL,
  lambda_min_ratio = 1e-05,
  nlambda = 150,
  thresh = 1e-06,
  validate_search = TRUE,
  seed = NA,
  search_terms = NULL,
  search_out = NULL,
  parallel = getOption("projpred.parallel_cv", FALSE),
  ...
)
```

Arguments

object	An object of class refmodel (returned by get_refmodel() or init_refmodel()) or an object that can be passed to argument object of get_refmodel().
...	For cv_varsel.default(): Arguments passed to get_refmodel() as well as to cv_varsel.refmodel(). For cv_varsel.vsel(): Arguments passed to cv_varsel.refmodel(). For cv_varsel.refmodel(): Arguments passed to the divergence minimizer (see argument div_minimizer of init_refmodel() as well as section "Draw-wise divergence minimizers" of projpred-package) when refitting the submodels for the performance evaluation (if refit_prj is TRUE).
cv_method	The CV method, either "LOO" or "kfold". In the "LOO" case, a Pareto-smoothed importance sampling leave-one-out CV (PSIS-LOO CV) is performed, which avoids refitting the reference model nloo times (in contrast to a standard LOO-CV). In the "kfold" case, a K-fold CV is performed. See also section "Note" below.
nloo	Only relevant if cv_method = "LOO" and validate_search = TRUE. If nloo > 0 is smaller than the number of all observations, full LOO-CV (i.e., PSIS-LOO CV

with validate_search = TRUE and with nloo = n where n denotes the number of all observations) is approximated by subsampled LOO-CV, i.e., by combining the fast (i.e., validate_search = FALSE) LOO result for the selected models and nloo leave-one-out searches using the difference estimator with simple random sampling (SRS) without replacement (WOR) (Magnusson et al., 2020). Smaller nloo values lead to faster computation, but higher uncertainty in the evaluation part. If NULL, all observations are used (as by default). Note that performance statistic "auc" (see argument stats of summary.vsel() and plot.vsel()) is not supported in case of subsampled LOO-CV. Furthermore, option "best" for argument baseline of summary.vsel() and plot.vsel() is not supported in case of subsampled LOO-CV.

K — Only relevant if cv_method = "kfold" and if cvfits is NULL (which is the case for reference model objects created by get_refmodel.stanreg() or brms::get_refmodel.brmsfit()) Number of folds in K-fold CV.

cvfits — Only relevant if cv_method = "kfold". The same as argument cvfits of init_refmodel(), but repeated here so that output from run_cvfun() can be inserted here straightforwardly.

validate_search — A single logical value indicating whether to cross-validate also the search part, i.e., whether to run the search separately for each CV fold (TRUE) or not (FALSE). With FALSE, the computation is faster, but the predictive performance estimates of the selected submodels are optimistically biased. However, these fast biased estimates can be useful to obtain initial information on the usefulness of projection predictive variable selection.

method — The method for the search part. Possible options are "forward" for forward search and "L1" for L1 search. See also section "Details" below.

ndraws — Number of posterior draws used in the search part. Ignored if nclusters is not NULL or in case of L1 search (because L1 search always uses a single cluster). If both (nclusters and ndraws) are NULL, the number of posterior draws from the reference model is used for ndraws. See also section "Details" below.

nclusters — Number of clusters of posterior draws used in the search part. Ignored in case of L1 search (because L1 search always uses a single cluster). For the meaning of NULL, see argument ndraws. See also section "Details" below.

ndraws_pred — Only relevant if refit_prj is TRUE. Number of posterior draws used in the evaluation part. Ignored if nclusters_pred is not NULL. If both (nclusters_pred and ndraws_pred) are NULL, the number of posterior draws from the reference model is used for ndraws_pred. See also section "Details" below.

nclusters_pred — Only relevant if refit_prj is TRUE. Number of clusters of posterior draws used in the evaluation part. For the meaning of NULL, see argument ndraws_pred. See also section "Details" below.

refit_prj — For the evaluation part, should the projections onto the submodels along the predictor ranking be performed again using ndraws_pred draws or nclusters_pred clusters (TRUE) or should their projections from the search part, which used ndraws draws or nclusters clusters, be re-used (FALSE)?

nterms_max — Maximum submodel size (number of predictor terms) up to which the search is continued. If NULL, then min(19, D) is used where D is the number of terms

in the reference model (or in search_terms, if supplied). Note that nterms_max does not count the intercept, so use nterms_max = 0 for the intercept-only model. (Correspondingly, D above does not count the intercept.)

penalty — Only relevant for L1 search. A numeric vector determining the relative penalties or costs for the predictors. A value of 0 means that those predictors have no cost and will therefore be selected first, whereas Inf means those predictors will never be selected. If NULL, then 1 is used for each predictor.

verbose — A single integer value from the set $\{0, 1, 2, 3, 4\}$ (for varsel(), 3 and 4 have the same effect), indicating how much information (if any) to print out during the computations. Higher values indicate that more information should be printed, 0 deactivates the verbose mode. Internally, argument verbose is coerced to integer via as.integer(), so technically, a single logical value or a single numeric value work as well.

search_control — A list of "control" arguments (i.e., tuning parameters) for the search. In case of forward search, these arguments are passed to the divergence minimizer (see argument div_minimizer of init_refmodel() as well as section "Draw-wise divergence minimizers" of projpred-package). In case of forward search, NULL causes ... to be used not only for the performance evaluation, but also for the search. In case of L1 search, possible arguments are:

- lambda_min_ratio: Ratio between the smallest and largest lambda in the L1-penalized search (default: 1e-5). This parameter essentially determines how long the search is carried out, i.e., how large submodels are explored. No need to change this unless the program gives a warning about this.
- nlambda: Number of values in the lambda grid for L1-penalized search (default: 150). No need to change this unless the program gives a warning about this.
- thresh: Convergence threshold when computing the L1 path (default: 1e-6). Usually, there is no need to change this.

lambda_min_ratio — Deprecated (please use search_control instead). Only relevant for L1 search. Ratio between the smallest and largest lambda in the L1-penalized search. This parameter essentially determines how long the search is carried out, i.e., how large submodels are explored. No need to change this unless the program gives a warning about this.

nlambda — Deprecated (please use search_control instead). Only relevant for L1 search. Number of values in the lambda grid for L1-penalized search. No need to change this unless the program gives a warning about this.

thresh — Deprecated (please use search_control instead). Only relevant for L1 search. Convergence threshold when computing the L1 path. Usually, there is no need to change this.

seed — Pseudorandom number generation (PRNG) seed by which the same results can be obtained again if needed. Passed to argument seed of set.seed(), but can also be NA to not call set.seed() at all. If not NA, then the PRNG state is reset (to the state before calling cv_varsel()) upon exiting cv_varsel(). Here, seed is used for clustering the reference model's posterior draws (if !is.null(nclusters) or !is.null(nclusters_pred)), for subsampling PSIS-LOO CV folds (if nloo

is smaller than the number of observations), for sampling the folds in K-fold CV, and for drawing new group-level effects when predicting from a multilevel submodel (however, not yet in case of a GAMM).

`search_terms` Only relevant for forward search. A custom character vector of predictor term blocks to consider for the search. Section "Details" below describes more precisely what "predictor term block" means. The intercept (`"1"`) is always included internally via `union()`, so there's no difference between including it explicitly or omitting it. The default `search_terms` considers all the terms in the reference model's formula.

`search_out` Intended for internal use.

`parallel` A single logical value indicating whether to run costly parts of the CV in parallel (`TRUE`) or not (`FALSE`). See also section "Note" below as well as section "Parallelization" in projpred-package.

Details

Arguments `ndraws`, `nclusters`, `nclusters_pred`, and `ndraws_pred` are automatically truncated at the number of posterior draws in the reference model (which is `1` for `datafits`). Using less draws or clusters in `ndraws`, `nclusters`, `nclusters_pred`, or `ndraws_pred` than posterior draws in the reference model may result in slightly inaccurate projection performance. Increasing these arguments affects the computation time linearly.

For argument `method`, there are some restrictions: For a reference model with multilevel or additive formula terms or a reference model set up for the augmented-data projection, only the forward search is available. Furthermore, argument `search_terms` requires a forward search to take effect.

L1 search is faster than forward search, but forward search may be more accurate. Furthermore, forward search may find a sparser model with comparable performance to that found by L1 search, but it may also overfit when more predictors are added. This overfit can be detected by running search validation (see `cv_varsel()`).

An L1 search may select an interaction term before all involved lower-order interaction terms (including main-effect terms) have been selected. In **projpred** versions > 2.6.0, the resulting predictor ranking is automatically modified so that the lower-order interaction terms come before this interaction term, but if this is conceptually undesired, choose the forward search instead.

The elements of the `search_terms` character vector don't need to be individual predictor terms. Instead, they can be building blocks consisting of several predictor terms connected by the `+` symbol. To understand how these building blocks work, it is important to know how **projpred**'s forward search works: It starts with an empty vector `chosen` which will later contain already selected predictor terms. Then, the search iterates over model sizes $j \in \{0, ..., J\}$ (with J denoting the maximum submodel size, not counting the intercept). The candidate models at model size j are constructed from those elements from `search_terms` which yield model size j when combined with the `chosen` predictor terms. Note that sometimes, there may be no candidate models for model size j. Also note that internally, `search_terms` is expanded to include the intercept (`"1"`), so the first step of the search (model size 0) always consists of the intercept-only model as the only candidate.

As a `search_terms` example, consider a reference model with formula `y ~ x1 + x2 + x3`. Then, to ensure that `x1` is always included in the candidate models, specify `search_terms = c("x1", "x1 + x2", "x1 + x3", "x1 + x2 + x3")` (or, in a simpler way that leads to the same results, `search_terms = c("x1", "x1 + x2", "x1 + x3")`, for which helper function `force_search_terms()` exists). This

search would start with `y ~ 1` as the only candidate at model size 0. At model size 1, `y ~ x1` would be the only candidate. At model size 2, `y ~ x1 + x2` and `y ~ x1 + x3` would be the two candidates. At the last model size of 3, `y ~ x1 + x2 + x3` would be the only candidate. As another example, to exclude `x1` from the search, specify `search_terms = c("x2", "x3", "x2 + x3")` (or, in a simpler way that leads to the same results, `search_terms = c("x2", "x3")`).

Value

An object of class `vsel`. The elements of this object are not meant to be accessed directly but instead via helper functions (see the main vignette and projpred-package).

Note

If `validate_search` is `FALSE`, the search is not included in the CV so that only a single full-data search is run. If the number of observations is large, the fast PSIS-LOO CV along the full-data search path is likely to be accurate. If the number of observations is small or moderate, the fast PSIS-LOO CV along the full-data search path is likely to have optimistic bias in the middle of the search path. This result can be used to guide further actions and the optimistic bias can be greatly reduced by using `validate_search = TRUE`.

PSIS uses the Pareto-$\hat{k}$ diagnostic to assess the reliability of PSIS-LOO CV. Global option `projpred.warn_psis` (default `TRUE`) controls whether the Pareto-$\hat{k}$ diagnostics may result in warnings. See loo::loo-glossary for how to interpret the Pareto-$\hat{k}$ values and the warning thresholds. **projpred** does not support the usually recommended moment-matching (see `loo::loo_moment_match()` and `brms::loo_moment_match()`), mixture importance sampling (`vignette("loo2-mixis", package="loo")`), or `reloo`-ing (`brms::reloo()`). If the reference model PSIS-LOO CV Pareto-$\hat{k}$ values are good, but there are high Pareto-$\hat{k}$ values for the projected models, you can try increasing the number of draws used for the PSIS-LOO CV (`ndraws` in case of `refit_prj = FALSE`; `ndraws_pred` in case of `refit_prj = TRUE`). If increasing the number of draws does not help and if the reference model PSIS-LOO CV Pareto-$\hat{k}$ values are high, and the reference model PSIS-LOO CV results change substantially when using moment-matching, mixture importance sampling, or `reloo`-ing, we recommend to use K-fold CV within `projpred`.

For PSIS-LOO CV, **projpred** calls `loo::psis()` (or, exceptionally, `loo::sis()`, see below) with `r_eff = NA`. This is only a problem if there was extreme autocorrelation between the MCMC iterations when the reference model was built. In those cases however, the reference model should not have been used anyway, so we don't expect **projpred**'s `r_eff = NA` to be a problem.

PSIS cannot be used if the number of draws or clusters is too small. In such cases, **projpred** resorts to standard importance sampling (SIS) and shows a message about this. Throughout the documentation, the term "PSIS" is used even though in fact, **projpred** resorts to SIS in these special cases. If SIS is used, check that the reference model PSIS-LOO CV Pareto-$\hat{k}$ values are good.

With `parallel = TRUE`, costly parts of **projpred**'s CV can be run in parallel. Costly parts are the fold-wise searches and performance evaluations in case of `validate_search = TRUE`. (Note that in case of K-fold CV, the K reference model refits are not affected by argument `parallel`; only **projpred**'s CV is affected.) The parallelization is powered by the **foreach** package. Thus, any parallel (or sequential) backend compatible with **foreach** can be used, e.g., the backends from packages **doParallel**, **doMPI**, or **doFuture**. For GLMs, this CV parallelization should work reliably, but for other models (such as GLMMs), it may lead to excessive memory usage which in turn may crash the R session (on Unix systems, setting an appropriate memory limit via `unix::rlimit_as()` may avoid crashing the whole machine). However, the problem of excessive memory usage is less

pronounced for the CV parallelization than for the projection parallelization described in projpred-package. In that regard, the CV parallelization is recommended over the projection parallelization.

References

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See Also

varsel()

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 1000, refresh = 0, seed = 9876
)

# Run cv_varsel() (with L1 search and small values for `K`, `nterms_max`, and
# `nclusters_pred`, but only for the sake of speed in this example; this is
# not recommended in general):
cvvs <- cv_varsel(fit, method = "L1", cv_method = "kfold", K = 2,
                  nterms_max = 3, nclusters_pred = 10, seed = 5555)
# Now see, for example, `?print.vsel`, `?plot.vsel`, `?suggest_size.vsel`,
# and `?ranking` for possible post-processing functions.
```

df_binom *Binomial toy example*

Description

Binomial toy example

Usage

```
data(df_binom)
```

Format

A simulated classification dataset containing 100 observations.

y response, 0 or 1.

x predictors, 30 in total.

Source

https://web.stanford.edu/~hastie/glmnet/glmnetData/BNExample.RData

df_gaussian *Gaussian toy example*

Description

Gaussian toy example

Usage

```
data(df_gaussian)
```

Format

A simulated regression dataset containing 100 observations.

y response, real-valued.

x predictors, 20 in total. Mean and SD are approximately 0 and 1, respectively.

Source

https://web.stanford.edu/~hastie/glmnet/glmnetData/QSExample.RData

extend_family *Extend a family*

Description

This function adds some internally required elements to an object of class `family` (see, e.g., `family()`). It is called internally by `init_refmodel()`, so you will rarely need to call it yourself.

Usage

```
extend_family(
  family,
  latent = FALSE,
  latent_y_unqs = NULL,
  latent_ilink = NULL,
  latent_ll_oscale = NULL,
  latent_ppd_oscale = NULL,
  augdat_y_unqs = NULL,
  augdat_link = NULL,
  augdat_ilink = NULL,
  augdat_args_link = list(),
  augdat_args_ilink = list(),
  ...
)
```

Arguments

`family`	An object of class `family`.
`latent`	A single logical value indicating whether to use the latent projection (`TRUE`) or not (`FALSE`). Note that setting `latent = TRUE` causes all arguments starting with `augdat_` to be ignored.
`latent_y_unqs`	Only relevant for a latent projection where the original response space has finite support (i.e., the original response values may be regarded as categories), in which case this needs to be the character vector of unique response values (which will be assigned to `family$cats` internally) or may be left at `NULL` (so that **projpred** will try to infer it from `family$cats`). See also section "Latent projection" below.
`latent_ilink`	Only relevant for the latent projection, in which case this needs to be the inverse-link function. If the original response family was the `binomial()` or the `poisson()` family, then `latent_ilink` can be `NULL`, in which case an internal default will be used. Can also be `NULL` in all other cases, but then an internal default based on `family$linkinv` will be used which might not work for all families. See also section "Latent projection" below.
`latent_ll_oscale`	Only relevant for the latent projection, in which case this needs to be the function computing response-scale (not latent-scale) log-likelihood values. If `!is.null(family$cats)`

(after taking `latent_y_unqs` into account) or if the original response family was the `binomial()` or the `poisson()` family, then `latent_ll_oscale` can be `NULL`, in which case an internal default will be used. Can also be `NULL` in all other cases, but then downstream functions will have limited functionality (a message thrown by `extend_family()` will state what exactly won't be available). See also section "Latent projection" below.

`latent_ppd_oscale`
: Only relevant for the latent projection, in which case this needs to be the function sampling response values given latent predictors that have been transformed to response scale using `latent_ilink`. If `!is.null(family$cats)` (after taking `latent_y_unqs` into account) or if the original response family was the `binomial()` or the `poisson()` family, then `latent_ppd_oscale` can be `NULL`, in which case an internal default will be used. Can also be `NULL` in all other cases, but then downstream functions will have limited functionality (a message thrown by `extend_family()` will state what exactly won't be available). See also section "Latent projection" below. Note that although this function has the abbreviation "PPD" in its name (which stands for "posterior predictive distribution"), **projpred** currently only uses it in `proj_predict()`, i.e., for sampling from what would better be termed posterior-projection predictive distribution (PPPD).

`augdat_y_unqs`
: Only relevant for augmented-data projection, in which case this needs to be the character vector of unique response values (which will be assigned to `family$cats` internally) or may be left at `NULL` if `family$cats` is already non-`NULL`. See also section "Augmented-data projection" below.

`augdat_link`
: Only relevant for augmented-data projection, in which case this needs to be the link function. Use `NULL` for the traditional projection. See also section "Augmented-data projection" below.

`augdat_ilink`
: Only relevant for augmented-data projection, in which case this needs to be the inverse-link function. Use `NULL` for the traditional projection. See also section "Augmented-data projection" below.

`augdat_args_link`
: Only relevant for augmented-data projection, in which case this may be a named `list` of arguments to pass to the function supplied to `augdat_link`.

`augdat_args_ilink`
: Only relevant for augmented-data projection, in which case this may be a named `list` of arguments to pass to the function supplied to `augdat_ilink`.

`...`
: Ignored (exists only to swallow up further arguments which might be passed to this function).

Details

In the following, N, C_{cat}, C_{lat}, S_{ref}, and S_{prj} from help topic refmodel-init-get are used. Note that N does not necessarily denote the number of original observations; it can also refer to new observations. Furthermore, let S denote either S_{ref} or S_{prj}, whichever is appropriate in the context where it is used.

Value

The `family` object extended in the way needed by **projpred**.

Augmented-data projection

As their first input, the functions supplied to arguments `augdat_link` and `augdat_ilink` have to accept:

- For `augdat_link`: an $S \times N \times C_{\text{cat}}$ array containing the probabilities for the response categories. The order of the response categories is the same as in `family$cats` (see argument `augdat_y_unqs`).
- For `augdat_ilink`: an $S \times N \times C_{\text{lat}}$ array containing the linear predictors.

The return value of these functions needs to be:

- For `augdat_link`: an $S \times N \times C_{\text{lat}}$ array containing the linear predictors.
- For `augdat_ilink`: an $S \times N \times C_{\text{cat}}$ array containing the probabilities for the response categories. The order of the response categories has to be the same as in `family$cats` (see argument `augdat_y_unqs`).

For the augmented-data projection, the response vector resulting from `extract_model_data` (see `init_refmodel()`) is coerced to a `factor` (using `as.factor()`) at multiple places throughout this package. Inside of `init_refmodel()`, the levels of this `factor` have to be identical to `family$cats` (*after* applying `extend_family()` inside of `init_refmodel()`). Everywhere else, these levels have to be a subset of `<refmodel>$family$cats` (where `<refmodel>` is an object resulting from `init_refmodel()`). See argument `augdat_y_unqs` for how to control `family$cats`.

For ordinal **brms** families, be aware that the submodels (onto which the reference model is projected) currently have the following restrictions:

- The discrimination parameter `disc` is not supported (i.e., it is a constant with value 1).
- The thresholds are `"flexible"` (see `brms::brmsfamily()`).
- The thresholds do not vary across the levels of a `factor`-like variable (see argument `gr` of `brms::resp_thres()`).
- The `"probit_approx"` link is replaced by `"probit"`.

For the `brms::categorical()` family, be aware that:

- For multilevel submodels, the group-level effects are allowed to be correlated between different response categories.
- For multilevel submodels, **mclogit** versions < 0.9.4 may throw the error `'a' (<number> x 1) must be square`. Updating **mclogit** to a version >= 0.9.4 should fix this.

Latent projection

The function supplied to argument `latent_ilink` needs to have the prototype

```
latent_ilink(lpreds, cl_ref, wdraws_ref = rep(1, length(cl_ref)))
```

where:

- `lpreds` accepts an $S \times N$ matrix containing the linear predictors.
- `cl_ref` accepts a numeric vector of length S_{ref}, containing **projpred**'s internal cluster indices for these draws.
- `wdraws_ref` accepts a numeric vector of length S_{ref}, containing weights for these draws. These weights should be treated as not being normalized (i.e., they don't necessarily sum to 1).

The return value of `latent_ilink` needs to contain the linear predictors transformed to the original response space, with the following structure:

- If `is.null(family$cats)` (after taking `latent_y_unqs` into account): an $S \times N$ matrix.
- If `!is.null(family$cats)` (after taking `latent_y_unqs` into account): an $S \times N \times C_{\text{cat}}$ array. In that case, `latent_ilink` needs to return *probabilities* (for the response categories given in `family$cats`, after taking `latent_y_unqs` into account).

The function supplied to argument `latent_ll_oscale` needs to have the prototype

```
latent_ll_oscale(ilpreds, dis, y_oscale, wobs = rep(1, ncol(ilpreds)),
                 cens, cl_ref, wdraws_ref = rep(1, length(cl_ref)))
```

where:

- `ilpreds` accepts the return value from `latent_ilink`.
- `dis` accepts a vector of length S containing dispersion parameter draws.
- `y_oscale` accepts a vector of length N containing response values on the original response scale.
- `wobs` accepts a numeric vector of length N containing observation weights.
- `cens` accepts a vector containing censoring indicators for the observations for which to calculate the response-scale log-likelihood values (i.e., for the observations from the second dimension of `ilpreds`). When calling `latent_ll_oscale`, **projpred** always specifies argument `cens` (with value `NULL` if attribute `cens_var` of `latent_ll_oscale` does not exist or is `NULL`), so a default value of `cens` can be defined, but will not be used.
- `cl_ref` accepts the same input as argument `cl_ref` of `latent_ilink`.
- `wdraws_ref` accepts the same input as argument `wdraws_ref` of `latent_ilink`.

In case of censoring (in the response values, i.e., survival or time-to-event analysis), the latent projection (with response-scale analyses) can be used by setting an attribute `cens_var` of the `latent_ll_oscale` function to a right-hand side formula with the name of the variable containing the censoring indicators (e.g., `0` = uncensored, `1` = censored) on its right-hand side. This variable named in the `cens_var` attribute is then retrieved (internally, whenever calling the `latent_ll_oscale` function) from the original dataset (possibly subsetted to the observations corresponding to the second dimension of `ilpreds`), `newdata`, or element `data` from `varsel()`'s argument `d_test`, whichever is applicable. The content of the retrieved variable is passed to argument `cens` of the `latent_ll_oscale` function. Note that only the performance statistics `"elpd"`, `"mlpd"`, and `"gmpd"` take censoring into account (on response scale).

The return value of `latent_ll_oscale` needs to be an $S \times N$ matrix containing the response-scale (not latent-scale) log-likelihood values for the N observations from its inputs.

The function supplied to argument `latent_ppd_oscale` needs to have the prototype

```
latent_ppd_oscale(ilpreds_resamp, dis_resamp,
                  wobs = rep(1, ncol(ilpreds_resamp)), cl_ref,
                  wdraws_ref = rep(1, length(cl_ref)), idxs_prjdraws)
```

where:

- `ilpreds_resamp` accepts the return value from `latent_ilink`, but possibly with resampled (clustered) draws (see argument `nresample_clusters` of `proj_predict()`).
- `dis_resamp` accepts a vector of length `dim(ilpreds_resamp)[1]` containing dispersion parameter draws, possibly resampled (in the same way as the draws in `ilpreds_resamp`, see also argument `idxs_prjdraws`).
- `wobs` accepts a numeric vector of length N containing observation weights.
- `cl_ref` accepts the same input as argument `cl_ref` of `latent_ilink`.
- `wdraws_ref` accepts the same input as argument `wdraws_ref` of `latent_ilink`.
- `idxs_prjdraws` accepts a numeric vector of length `dim(ilpreds_resamp)[1]` containing the resampled indices of the projected draws (i.e., these indices are values from the set $\{1, ..., $ `dim(ilpreds)[1]`$\}$ where `ilpreds` denotes the return value of `latent_ilink`).

The return value of `latent_ppd_oscale` needs to be a `dim(ilpreds_resamp)[1]` $\times N$ matrix containing the response-scale (not latent-scale) draws from the posterior(-projection) predictive distributions for the N observations from its inputs.

If the bodies of these three functions involve parameter draws from the reference model which have not been projected (e.g., for `latent_ilink`, the thresholds in an ordinal model), `cl_agg()` is provided as a helper function for aggregating these reference model draws in the same way as the draws have been aggregated for the first argument of these functions (e.g., `lpreds` in case of `latent_ilink`).

In fact, the weights passed to argument `wdraws_ref` are nonconstant only in case of `cv_varsel()` with `cv_method = "LOO"` and `validate_search = TRUE`. In that case, the weights passed to this argument are the PSIS-LOO CV weights for one observation. Note that although argument `wdraws_ref` has the suffix `_ref`, `wdraws_ref` does not necessarily obtain weights for the *initial* reference model's posterior draws: In case of `cv_varsel()` with `cv_method = "kfold"`, these weights may refer to one of the K reference model refits (but in that case, they are constant anyway).

If `family$cats` is not `NULL` (after taking `latent_y_unqs` into account), then the response vector resulting from `extract_model_data` (see `init_refmodel()`) is coerced to a `factor` (using `as.factor()`) at multiple places throughout this package. Inside of `init_refmodel()`, the levels of this `factor` have to be identical to `family$cats` (*after* applying `extend_family()` inside of `init_refmodel()`). Everywhere else, these levels have to be a subset of `<refmodel>$family$cats` (where `<refmodel>` is an object resulting from `init_refmodel()`).

`extra-families` *Extra family objects*

Description

Family objects not in the set of default `family` objects.

Usage

```
Student_t(link = "identity", nu = 3)
```

Arguments

link	Name of the link function. In contrast to the default family objects, this has to be a character string here.
nu	Degrees of freedom for the Student-t distribution.

Value

A family object analogous to those described in family.

Note

Support for the Student_t() family is still experimental.

---

force_search_terms *Force search terms*

Description

A helper function to construct the input for argument search_terms of varsel() or cv_varsel() if certain predictor terms should be forced to be selected first whereas other predictor terms are optional (i.e., they are subject to the variable selection, but only after the inclusion of the "forced" terms).

Usage

```
force_search_terms(forced_terms, optional_terms)
```

Arguments

forced_terms	A character vector of predictor terms that should be selected first.
optional_terms	A character vector of predictor terms that should be subject to the variable selection after the inclusion of the "forced" terms.

Value

A character vector that may be used as input for argument search_terms of varsel() or cv_varsel().

See Also

varsel(), cv_varsel()

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# We will force X1 and X2 to be selected first:
search_terms_forced <- force_search_terms(
  forced_terms = paste0("X", 1:2),
  optional_terms = paste0("X", 3:5)
)

# Run varsel() (here without cross-validation and with small values for
# `nterms_max`, `nclusters`, and `nclusters_pred`, but only for the sake of
# speed in this example; this is not recommended in general):
vs <- varsel(fit, nclusters = 5, nclusters_pred = 10,
             search_terms = search_terms_forced, seed = 5555)
# Now see, for example, `?print.vsel`, `?plot.vsel`, `?suggest_size.vsel`,
# and `?ranking` for possible post-processing functions.
```

`mesquite` *Mesquite data set*

Description

The mesquite bushes yields dataset from Gelman and Hill (2006) (https://sites.stat.columbia.edu/gelman/arm/).

Usage

```
data(mesquite)
```

Format

The response variable is the total weight (in grams) of photosynthetic material as derived from actual harvesting of the bush. The predictor variables are:

diam1 diameter of the canopy (the leafy area of the bush) in meters, measured along the longer axis of the bush.

diam2 canopy diameter measured along the shorter axis.

canopy height height of the canopy.

total height total height of the bush.

density plant unit density (# of primary stems per plant unit).

group group of measurements (0 for the first group, 1 for the second group).

Source

https://sites.stat.columbia.edu/gelman/arm/examples/mesquite/mesquite.dat

References

Gelman, Andrew, and Jennifer Hill. 2006. *Data Analysis Using Regression and Multilevel/Hierarchical Models*. Cambridge, UK: Cambridge University Press. doi:10.1017/CBO9780511790942.

`performances` *Predictive performance results*

Description

Retrieves the predictive performance summaries after running `varsel()` or `cv_varsel()`. These summaries are computed by `summary.vsel()`, so the main method of `performances()` is `performances.vselsummary()` (objects of class `vselsummary` are returned by `summary.vsel()`). As a shortcut method, `performances.vsel()` is provided as well (objects of class `vsel` are returned by `varsel()` and `cv_varsel()`). For a graphical representation, see `plot.vsel()`.

Usage

```
performances(object, ...)

## S3 method for class 'vselsummary'
performances(object, ...)

## S3 method for class 'vsel'
performances(object, ...)
```

Arguments

`object`	The object from which to retrieve the predictive performance results. Possible classes may be inferred from the names of the corresponding methods (see also the description).
`...`	For `performances.vsel()`: arguments passed to `summary.vsel()`. For `performances.vselsummary()` currently ignored.

Value

An object of class `performances` which is a `list` with the following elements:

- `submodels`: The predictive performance results for the submodels, as a `data.frame`.
- `reference_model`: The predictive performance results for the reference model, as a named vector.

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Run varsel() (here without cross-validation, with L1 search, and with small
# values for `nterms_max` and `nclusters_pred`, but only for the sake of
# speed in this example; this is not recommended in general):
vs <- varsel(fit, method = "L1", nterms_max = 3, nclusters_pred = 10,
             seed = 5555)
print(performances(vs))
```

---

plot.cv_proportions *Plot ranking proportions from fold-wise predictor rankings*

Description

Plots the ranking proportions (see `cv_proportions()`) from the fold-wise predictor rankings in a cross-validation with fold-wise searches. This is a visualization of the *transposed* matrix returned by `cv_proportions()`. The proportions printed as text inside of the colored tiles are rounded to whole percentage points (the plotted proportions themselves are not rounded).

Usage

```
## S3 method for class 'cv_proportions'
plot(
  x,
  text_angle = getOption("projpred.plot_cv_proportions_text_angle", NULL),
  ...
)

## S3 method for class 'ranking'
plot(x, ...)
```

Arguments

x	For `plot.cv_proportions()`: an object of class `cv_proportions` (returned by `cv_proportions()`, possibly with `cumulate = TRUE`). For `plot.ranking()`: an object of class `ranking` (returned by `ranking()`) that `cv_proportions()` will be applied to internally before then calling `plot.cv_proportions()`.

text_angle	Passed to argument angle of ggplot2::element_text() for the y-axis tick labels. In case of long predictor names, text_angle = 45 might be helpful (for example).
...	For plot.ranking(): arguments passed to cv_proportions.ranking() and plot.cv_proportions(). For plot.cv_proportions(): currently ignored.

Value

A **ggplot2** plotting object (of class gg and ggplot).

Author(s)

Idea and original code by Aki Vehtari. Slight modifications of the original code by Frank Weber, Yann McLatchie, and Sölvi Rögnvaldsson. Final implementation in **projpred** by Frank Weber.

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 1000, refresh = 0, seed = 9876
)

# Run cv_varsel() (with L1 search and small values for `K`, `nterms_max`, and
# `nclusters_pred`, but only for the sake of speed in this example; this is
# not recommended in general):
cvvs <- cv_varsel(fit, method = "L1", cv_method = "kfold", K = 2,
                  nterms_max = 3, nclusters_pred = 10, seed = 5555)

# Extract predictor rankings:
rk <- ranking(cvvs)

# Compute ranking proportions:
pr_rk <- cv_proportions(rk)

# Visualize the ranking proportions:
gg_pr_rk <- plot(pr_rk)
print(gg_pr_rk)

# Since the object returned by plot.cv_proportions() is a standard ggplot2
# plotting object, you can modify the plot easily, e.g., to remove the
# legend:
print(gg_pr_rk + ggplot2::theme(legend.position = "none"))
```

plot.vsel *Plot predictive performance*

Description

This is the plot() method for vsel objects (returned by varsel() or cv_varsel()). It visualizes the predictive performance of the reference model (possibly also that of some other "baseline" model) and that of the submodels along the full-data predictor ranking. Basic information about the (CV) variability in the ranking of the predictors is included as well (if available; inferred from cv_proportions()). For a tabular representation, see summary.vsel() and performances().

Usage

```
## S3 method for class 'vsel'
plot(
  x,
  nterms_max = NULL,
  stats = "elpd",
  deltas = FALSE,
  alpha = 2 * pnorm(-1),
  baseline = if (!inherits(x$refmodel, "datafit")) "ref" else "best",
  thres_elpd = NA,
  resp_oscale = TRUE,
  point_size = getOption("projpred.plot_vsel_point_size", 3),
  bar_thickness = getOption("projpred.plot_vsel_bar_thickness", 1),
 ranking_nterms_max = getOption("projpred.plot_vsel_ranking_nterms_max", NULL),
 ranking_abbreviate = getOption("projpred.plot_vsel_ranking_abbreviate", FALSE),
 ranking_abbreviate_args = getOption("projpred.plot_vsel_ranking_abbreviate_args",
    list()),
  ranking_repel = getOption("projpred.plot_vsel_ranking_repel", NULL),
 ranking_repel_args = getOption("projpred.plot_vsel_ranking_repel_args", list()),
  ranking_colored = getOption("projpred.plot_vsel_ranking_colored", FALSE),
 show_cv_proportions = getOption("projpred.plot_vsel_show_cv_proportions", FALSE),
  cumulate = FALSE,
  text_angle = getOption("projpred.plot_vsel_text_angle", 45),
 size_position = getOption("projpred.plot_vsel_size_position", "primary_x_top"),
  ...
)
```

Arguments

x	An object of class vsel (returned by varsel() or cv_varsel()).
nterms_max	Maximum submodel size (number of predictor terms) for which the performance statistics are calculated. Using NULL is effectively the same as length(ranking(object)$fulldata). Note that nterms_max does not count the intercept, so use nterms_max = 0 for the intercept-only model. For plot.vsel(), nterms_max must be at least 1.

stats — One or more character strings determining which performance statistics (i.e., utilities or losses) to estimate based on the observations in the evaluation (or "test") set (in case of cross-validation, these are all observations because they are partitioned into multiple test sets; in case of `varsel()` with `d_test = NULL`, these are again all observations because the test set is the same as the training set). Available statistics are:

- `"elpd"`: expected log (pointwise) predictive density (for a new dataset) (ELPD). Estimated by the sum of the observation-specific log predictive density values (with each of these predictive density values being a—possibly weighted—average across the parameter draws). For the corresponding uncertainty interval, a normal approximation is used.
- `"mlpd"`: mean log predictive density (MLPD), that is, the ELPD divided by the number of observations. For the corresponding uncertainty interval, a normal approximation is used.
- `"gmpd"`: geometric mean predictive density (GMPD), that is, `exp()` of the MLPD. The GMPD is especially helpful for discrete response families (because there, the GMPD is bounded by zero and one). For the corresponding standard error, the delta method is used. The corresponding uncertainty interval type is "exponentiated normal approximation" because the uncertainty interval bounds are the exponentiated uncertainty interval bounds of the MLPD.
- `"mse"`: mean squared error (only available in the situations mentioned in section "Details" below). For the corresponding uncertainty interval, a log-normal approximation is used if `deltas` is `FALSE` and a normal approximation is used if `deltas` is `TRUE` (or `"mixed"`, in case of `plot.vsel()`).
- `"rmse"`: root mean squared error (only available in the situations mentioned in section "Details" below). For the corresponding standard error, the delta method is used. For the corresponding uncertainty interval, a log-normal approximation is used if `deltas` is `FALSE` and a normal approximation is used if `deltas` is `TRUE` (or `"mixed"`, in case of `plot.vsel()`).
- `"R2"`: R-squared, i.e., coefficient of determination (only available in the situations mentioned in section "Details" below). For the corresponding standard error, the delta method is used. For the corresponding uncertainty interval, a normal approximation is used.
- `"acc"` (or its alias, `"pctcorr"`): classification accuracy (only available in the situations mentioned in section "Details" below). By "classification accuracy", we mean the proportion of correctly classified observations. For this, the response category ("class") with highest probability (the probabilities are model-based) is taken as the prediction ("classification") for an observation. For the corresponding uncertainty interval, a normal approximation is used.
- `"auc"`: area under the ROC curve (only available in the situations mentioned in section "Details" below). For the corresponding standard error and lower and upper uncertainty interval bounds, bootstrapping is used. Not supported in case of subsampled LOO-CV (see argument `nloo` of `cv_varsel()`).

deltas — May be set to `FALSE`, `TRUE`, or `"mixed"`. If `FALSE`, the submodel performance statistics are plotted on their actual scale and the uncertainty bars match this

scale. If TRUE, the submodel statistics are plotted relatively to the baseline model (see argument baseline) and the uncertainty bars match this scale. For the GMPD, the term "relatively" refers to the *ratio* vs. the baseline model (i.e., the submodel statistic divided by the baseline model statistic). For all other stats, "relatively" refers to the *difference* from the baseline model (i.e., the submodel statistic minus the baseline model statistic). If set to "mixed", the deltas = FALSE point estimates are combined with the uncertainty bars from the deltas = TRUE plot.

alpha — A number determining the (nominal) coverage 1 - alpha of the uncertainty intervals. For example, in case of a normal-approximation uncertainty interval, alpha = 2 * pnorm(-1) corresponds to a uncertainty interval stretching by one standard error on either side of the point estimate.

baseline — For summary.vsel(): Only relevant if deltas is TRUE. For plot.vsel(): Always relevant. Either "ref" or "best", indicating whether the baseline is the reference model or the best submodel found (in terms of stats[1]), respectively. In case of subsampled LOO-CV, baseline = "best" is not supported.

thres_elpd — Only relevant if any(stats %in% c("elpd", "mlpd", "gmpd")). The threshold for the ELPD difference (taking the submodel's ELPD minus the baseline model's ELPD) above which the submodel's ELPD is considered to be close enough to the baseline model's ELPD. An equivalent rule is applied in case of the MLPD and the GMPD. See suggest_size() for a formalization. Supplying NA deactivates this.

resp_oscale — Only relevant for the latent projection. A single logical value indicating whether to calculate the performance statistics on the original response scale (TRUE) or on latent scale (FALSE).

point_size — Passed to argument size of ggplot2::geom_point() and controls the size of the points.

bar_thickness — Passed to argument linewidth of ggplot2::geom_linerange() and controls the thickness of the uncertainty bars.

ranking_nterms_max — Maximum submodel size (number of predictor terms) for which the predictor names and the corresponding ranking proportions are added on the x-axis. Using NULL is effectively the same as using nterms_max. Using NA causes the predictor names and the corresponding ranking proportions to be omitted, which requires size_position = "primary_x_bottom". Note that ranking_nterms_max does not count the intercept, so ranking_nterms_max = 1 corresponds to the submodel consisting of the first (non-intercept) predictor term.

ranking_abbreviate — A single logical value indicating whether the predictor names in the full-data predictor ranking should be abbreviated by abbreviate() (TRUE) or not (FALSE). See also argument ranking_abbreviate_args and section "Value".

ranking_abbreviate_args — A list of arguments (except for names.arg) to be passed to abbreviate() in case of ranking_abbreviate = TRUE.

ranking_repel — Either NULL, "text", or "label". By NULL, the full-data predictor ranking and the corresponding ranking proportions are placed below the x-axis. By "text"

or "label", they are placed within the plotting area, using ggrepel::geom_text_repel() or ggrepel::geom_label_repel(), respectively. See also argument ranking_repel_args.

ranking_repel_args
: A list of arguments (except for mapping) to be passed to ggrepel::geom_text_repel() or ggrepel::geom_label_repel() in case of ranking_repel = "text" or ranking_repel = "label", respectively.

ranking_colored
: A single logical value indicating whether the points and the uncertainty bars should be gradient-colored according to the CV ranking proportions (TRUE, currently only works if show_cv_proportions is TRUE as well) or not (FALSE). The CV ranking proportions may be cumulated (see argument cumulate). Note that the point and the uncertainty bar at submodel size 0 (i.e., at the intercept-only model) are always colored in gray because the intercept is forced to be selected before any predictors are selected (in other words, the reason is that for submodel size 0, the question of variability across CV folds is not appropriate in the first place).

show_cv_proportions
: A single logical value indicating whether the CV ranking proportions (see cv_proportions()) should be displayed (TRUE) or not (FALSE).

cumulate
: Passed to argument cumulate of cv_proportions(). Affects the ranking proportions given on the x-axis (below the full-data predictor ranking).

text_angle
: Passed to argument angle of ggplot2::element_text() for the x-axis tick labels. Note that the default of argument angle in ggplot2::element_text() is NULL (which implies no rotation) whereas we use a default of text_angle = 45 here. If text_angle > 0 (< 0), the x-axis text is automatically right-aligned (left-aligned). If -90 < text_angle && text_angle < 90 && text_angle != 0, the x-axis text is also top-aligned. When controlling text_angle via global option projpred.plot_vsel_text_angle, keep in mind that a global option set to NULL is treated like an unset global option, so options(projpred.plot_vsel_text_angle = NULL) would result in text_angle = 45, not text_angle = 0.

size_position
: A single character string specifying the position of the submodel sizes. Either "primary_x_bottom" for including them in the x-axis tick labels, "primary_x_top" for putting them above the x-axis (the current default), or "secondary_x" for putting them into a secondary x-axis. Currently, "primary_x_top" and "secondary_x" may not be combined with ranking_nterms_max = NA (i.e., only "primary_x_bottom" works with ranking_nterms_max = NA).

...
: Arguments passed to the internal function which is used for bootstrapping (if applicable; see argument stats). Currently, relevant arguments are B (the number of bootstrap samples, defaulting to 2000) and seed (see set.seed(), but defaulting to NA so that set.seed() is not called within that function at all).

Details

The stats options "mse", "rmse", and "R2" are only available for:

- the traditional projection,
- the latent projection with resp_oscale = FALSE,

- the latent projection with `resp_oscale = TRUE` in combination with `<refmodel>$family$cats` being `NULL`.

The `stats` option `"acc"` (= `"pctcorr"`) is only available for:

- the `binomial()` family in case of the traditional projection,
- all families in case of the augmented-data projection,
- the `binomial()` family (on the original response scale) in case of the latent projection with `resp_oscale = TRUE` in combination with `<refmodel>$family$cats` being `NULL`,
- all families (on the original response scale) in case of the latent projection with `resp_oscale = TRUE` in combination with `<refmodel>$family$cats` being not `NULL`.

The `stats` option `"auc"` is only available for:

- the `binomial()` family in case of the traditional projection,
- the `binomial()` family (on the original response scale) in case of the latent projection with `resp_oscale = TRUE` in combination with `<refmodel>$family$cats` being `NULL`.

Note that the `stats` option `"auc"` is not supported in case of subsampled LOO-CV (see argument `nloo` of `cv_varsel()`).

Value

A **ggplot2** plotting object (of class `gg` and `ggplot`). If `ranking_abbreviate` is `TRUE`, the output of `abbreviate()` is stored in an attribute called `projpred_ranking_abbreviated` (to allow the abbreviations to be easily mapped back to the original predictor names).

Horizontal lines

As long as the reference model's performance is computable, it is always shown in the plot as a dashed red horizontal line. If `baseline = "best"`, the baseline model's performance is shown as a dotted black horizontal line. If `!is.na(thres_elpd)` and `any(stats %in% c("elpd", "mlpd", "gmpd"))`, the value supplied to `thres_elpd` (which is automatically adapted internally in case of the MLPD or the GMPD or `deltas = FALSE` or `deltas = "mixed"`) is shown as a dot-dashed gray horizontal line for the reference model and, if `baseline = "best"`, as a long-dashed green horizontal line for the baseline model.

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Run varsel() (here without cross-validation, with L1 search, and with small
```

```
# values for `nterms_max` and `nclusters_pred`, but only for the sake of
# speed in this example; this is not recommended in general):
vs <- varsel(fit, method = "L1", nterms_max = 3, nclusters_pred = 10,
             seed = 5555)
print(plot(vs))
```

---

pred-projection *Predictions from a submodel (after projection)*

Description

The proj_predict() function draws from the projected posterior predictive distribution of the submodel that the reference model has been projected onto. By definition, these draws have higher variability than draws of the expected value of the posterior predictive distribution computed by proj_epred(). This is because the aleatoric uncertainty from the data model is incorporated in proj_predict().

Usage

```
proj_linpred(
  object,
  newdata = NULL,
  offsetnew = NULL,
  weightsnew = NULL,
  filter_nterms = NULL,
  transform = FALSE,
  integrated = FALSE,
  allow_nonconst_wdraws_prj = return_draws_matrix,
  return_draws_matrix = FALSE,
  .seed = NA,
  ...
)

proj_predict(
  object,
  newdata = NULL,
  offsetnew = NULL,
  weightsnew = NULL,
  filter_nterms = NULL,
  nresample_clusters = 1000,
  return_draws_matrix = FALSE,
  .seed = NA,
  resp_oscale = TRUE,
  ...
)
```

```
proj_epred(
  object,
  newdata = NULL,
  offsetnew = NULL,
  weightsnew = NULL,
  filter_nterms = NULL,
  integrated = FALSE,
  allow_nonconst_wdraws_prj = return_draws_matrix,
  return_draws_matrix = FALSE,
  .seed = NA,
  ...
)
```

Arguments

object	An object returned by project() or an object that can be passed to argument object of project().
newdata	Passed to argument newdata of the reference model's extract_model_data function (see init_refmodel()). Provides the predictor (and possibly also the response) data for the new (or old) observations. May also be NULL for using the original dataset. If not NULL, any NAs will trigger an error.
offsetnew	Passed to argument orhs of the reference model's extract_model_data function (see init_refmodel()). Used to get the offsets for the new (or old) observations.
weightsnew	Passed to argument wrhs of the reference model's extract_model_data function (see init_refmodel()). Used to get the weights for the new (or old) observations.
filter_nterms	Only applies if object is an object returned by project(). In that case, filter_nterms can be used to filter object for only those elements (submodels) with a number of predictor terms in filter_nterms. Therefore, needs to be a numeric vector or NULL. If NULL, use all submodels.
transform	For proj_linpred() only (not applicable for proj_epred() which always uses transform = TRUE internally). A single logical value indicating whether the linear predictor should be transformed to response scale using the inverse-link function (TRUE) or not (FALSE). In case of the latent projection, argument transform is similar in spirit to argument resp_oscale from other functions and affects the scale of both output elements pred and lpd (see sections "Details" and "Value" below).
integrated	For proj_linpred() and proj_epred() only. A single logical value indicating whether the output should be averaged across the projected posterior draws (TRUE) or not (FALSE).
allow_nonconst_wdraws_prj	Only relevant for proj_linpred() and proj_epred() and only if integrated is FALSE. A single logical value indicating whether to allow projected draws with different (i.e., nonconstant) weights (TRUE) or not (FALSE). If return_draws_matrix is TRUE, allow_nonconst_wdraws_prj is internally set to TRUE as well. **CAUTION**: Expert use only because if set to TRUE, the weights of the projected

draws are stored in attributes wdraws_prj and handling these attributes requires special care (e.g., when subsetting the returned matrices).

return_draws_matrix
: A single logical value indicating whether to return an object (in case of proj_predict()) or objects (in case of proj_linpred() and proj_epred()) of class draws_matrix (see posterior::draws_matrix()). In case of proj_linpred() or proj_epred() and projected draws with nonconstant weights (as well as integrated being FALSE), posterior::weight_draws() is applied internally.

.seed
: Pseudorandom number generation (PRNG) seed by which the same results can be obtained again if needed. Passed to argument seed of set.seed(), but can also be NA to not call set.seed() at all. If not NA, then the PRNG state is reset (to the state before calling proj_linpred(), proj_epred(), or proj_predict()) upon exiting proj_linpred(), proj_epred(), or proj_predict(). Here, .seed is used for drawing new group-level effects in case of a multilevel submodel (however, not yet in case of a GAMM) and for drawing from the predictive distributions of the submodel(s) in case of proj_predict(). If a clustered projection was performed, then in proj_predict(), .seed is also used for drawing from the set of projected clusters of posterior draws (see argument nresample_clusters). If project() is called internally with seed = NA (or with seed being a lazily evaluated expression that uses the PRNG), then .seed also affects the PRNG usage there.

...
: Arguments passed to project() if object is not already an object returned by project().

nresample_clusters
: For proj_predict() with clustered projection (and nonconstant weights for the projected draws) only. Number of draws to return from the predictive distributions of the submodel(s). Not to be confused with argument nclusters of project(): nresample_clusters gives the number of draws (*with* replacement) from the set of clustered posterior draws after projection (with this set being determined by argument nclusters of project()).

resp_oscale
: Only relevant for the latent projection. A single logical value indicating whether to draw from the posterior-projection predictive distributions on the original response scale (TRUE) or on latent scale (FALSE).

Details

The proj_epred() function draws from the distribution of the expected value of the projected posterior predictive distribution. By definition, these predictions have smaller variability than the projected posterior predictions performed by proj_predict(). This is because only the epistemic uncertainty in the expected value of the projected posterior predictive distribution is incorporated in the draws, while the aleatoric uncertainty from the data model is not included. However, the estimated means of both methods averaged across draws should be very similar.

The proj_linpred() function draws from the projected posterior of the linear predictors, that is, draws before applying any link functions or other transformations. These linear predictors can also be transformed to response scale with argument transform = TRUE, which produces draws equivalent to draws produced by proj_epred(). Furthermore, proj_linpred() returns the corresponding log predictive density values if the (original or new) dataset contains response values.

All these predictions can be performed for the data used to fit the reference model or for new data. If the projection has not been performed yet, all three functions call `project()` internally to perform the projection. All three functions can also handle multiple submodels at once (for `objects` of class `vsel` or `objects` returned by a `project()` call to an object of class `vsel`; see `project()`).

Currently, `proj_predict()` ignores observation weights that are not equal to 1. A corresponding warning is thrown if this is the case.

In case of the latent projection and `transform = FALSE`:

- Output element `pred` contains the linear predictors without any modifications that may be due to the original response distribution (e.g., for a `brms::cumulative()` model, the ordered thresholds are not taken into account).
- Output element `lpd` contains the *latent* log predictive density values, i.e., those corresponding to the latent Gaussian distribution. If `newdata` is not `NULL`, this requires the latent response values to be supplied in a column called `.<response_name>` of `newdata` where `<response_name>` needs to be replaced by the name of the original response variable (if `<response_name>` contained parentheses, these have been stripped off by `init_refmodel()`; see the left-hand side of `formula(<refmodel>)`). For technical reasons, the existence of column `<response_name>` in `newdata` is another requirement (even though `.<response_name>` is actually used).

Value

In the following, S_{prj}, N, C_{cat}, and C_{lat} from help topic refmodel-init-get are used. (For `proj_linpred()` with `integrated = TRUE`, we have $S_{\text{prj}} = 1$.) Furthermore, let C denote either C_{cat} (if `transform = TRUE`) or C_{lat} (if `transform = FALSE`). Then, if the prediction is done for one submodel only (i.e., `length(nterms) == 1 || !is.null(predictor_terms)` in the explicit or implicit call to `project()`, see argument `object`):

- `proj_linpred()` returns a `list` with the following elements:
  - Element `pred` contains the actual predictions, i.e., the linear predictors, possibly transformed to response scale (depending on argument `transform`).
  - Element `lpd` is non-`NULL` only if `newdata` is `NULL` or if `newdata` contains response values in the corresponding column. In that case, it contains the log predictive density values (conditional on each of the projected parameter draws if `integrated = FALSE` and averaged across the projected parameter draws if `integrated = TRUE`).

  In case of (i) the traditional projection, (ii) the latent projection with `transform = FALSE`, or (iii) the latent projection with `transform = TRUE` and `<refmodel>$family$cats` (where `<refmodel>` is an object resulting from `init_refmodel()`; see also `extend_family()`'s argument `latent_y_unqs`) being `NULL`, both elements are $S_{\text{prj}} \times N$ matrices (converted to a—possibly weighted—`draws_matrix` if argument `return_draws_matrix` is `TRUE`, see the description of this argument). In case of (i) the augmented-data projection or (ii) the latent projection with `transform = TRUE` and `<refmodel>$family$cats` being not `NULL`, `pred` is an $S_{\text{prj}} \times N \times C$ array (if argument `return_draws_matrix` is `TRUE`, this array is "compressed" to an $S_{\text{prj}} \times (N \cdot C)$ matrix—with the columns consisting of C blocks of N rows—and then converted to a—possibly weighted—`draws_matrix`) and `lpd` is an $S_{\text{prj}} \times N$ matrix (converted to a—possibly weighted—`draws_matrix` if argument `return_draws_matrix` is `TRUE`). If `return_draws_matrix` is `FALSE` and `allow_nonconst_wdraws_prj` is `TRUE` and `integrated` is `FALSE` and the projected draws have nonconstant weights, then both `list` elements have the weights of these draws stored in an attribute `wdraws_prj`. (If `return_draws_matrix`,

allow_nonconst_wdraws_prj, and integrated are all FALSE, then projected draws with nonconstant weights cause an error.)

- proj_epred() is a wrapper around proj_linpred() with transform = TRUE and returns only the draws of the expected value of the projected posterior predictive distribution on the response scale (i.e., the pred element of the list returned by proj_linpred(), without the lpd element). The structure of the returned object is the same as that of the pred element described for proj_linpred() above.
- proj_predict() returns an $S_{\text{prj}} \times N$ matrix of predictions where S_{prj} denotes nresample_clusters in case of clustered projection (or, more generally, in case of projected draws with nonconstant weights). If argument return_draws_matrix is TRUE, the returned matrix is converted to a draws_matrix (see posterior::draws_matrix()). In case of (i) the augmented-data projection or (ii) the latent projection with resp_oscale = TRUE and <refmodel>$family$cats being not NULL, the returned matrix (or draws_matrix) has an attribute called cats (the character vector of response categories) and the values of the matrix (or draws_matrix) are the predicted indices of the response categories (these indices refer to the order of the response categories from attribute cats).

If the prediction is done for more than one submodel, the output from above is returned for each submodel, giving a named list with one element for each submodel (the names of this list being the numbers of predictor terms of the submodels when counting the intercept, too).

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Projection onto an arbitrary combination of predictor terms (with a small
# value for `ndraws`, but only for the sake of speed in this example; this
# is not recommended in general):
prj <- project(fit, predictor_terms = c("X1", "X3", "X5"), ndraws = 21,
               seed = 9182)

# Predictions (at the training points) from the submodel onto which the
# reference model was projected:
prjl <- proj_linpred(prj)
prje <- proj_epred(prj)
prjp <- proj_predict(prj, .seed = 7364)
```

predict.refmodel *Predictions or log posterior predictive densities from a reference model*

Description

This is the predict() method for refmodel objects (returned by get_refmodel() or init_refmodel()). It offers three types of output which are all based on the reference model and new (or old) observations: Either the linear predictor on link scale, the linear predictor transformed to response scale, or the log posterior predictive density.

Usage

```
## S3 method for class 'refmodel'
predict(
  object,
  newdata = NULL,
  ynew = NULL,
  offsetnew = NULL,
  weightsnew = NULL,
  type = "response",
  ...
)
```

Arguments

object	An object of class refmodel (returned by get_refmodel() or init_refmodel()).
newdata	Passed to argument newdata of the reference model's extract_model_data function (see init_refmodel()). Provides the predictor (and possibly also the response) data for the new (or old) observations. May also be NULL for using the original dataset. If not NULL, any NAs will trigger an error.
ynew	If not NULL, then this needs to be a vector of new (or old) response values. See also section "Value" below. In case of (i) the augmented-data projection or (ii) the latent projection with type = "response" and object$family$cats being not NULL, ynew is internally coerced to a factor (using as.factor()). The levels of this factor have to be a subset of object$family$cats (see extend_family()'s arguments augdat_y_unqs and latent_y_unqs, respectively).
offsetnew	Passed to argument orhs of the reference model's extract_model_data function (see init_refmodel()). Used to get the offsets for the new (or old) observations.
weightsnew	Passed to argument wrhs of the reference model's extract_model_data function (see init_refmodel()). Used to get the weights for the new (or old) observations.

type — Usually only relevant if `is.null(ynew)`, but for the latent projection, this also affects the `!is.null(ynew)` case (see below). The scale on which the predictions are returned, either `"link"` or `"response"` (see `predict.glm()` but note that `predict.refmodel()` does not adhere to the typical R convention of a default prediction on link scale). For both scales, the predictions are averaged across the posterior draws. In case of the latent projection, argument `type` is similar in spirit to argument `resp_oscale` from other functions: If (i) `is.null(ynew)`, then argument `type` affects the predictions as described above. In that case, note that `type = "link"` yields the linear predictors without any modifications that may be due to the original response distribution (e.g., for a `brms::cumulative()` model, the ordered thresholds are not taken into account). If (ii) `!is.null(ynew)`, then argument `type` also affects the scale of the log posterior predictive densities (`type = "response"` for the original response scale, `type = "link"` for the latent Gaussian scale).

... — Currently ignored.

Details

Argument `weightsnew` is only relevant if `!is.null(ynew)`.

In case of a multilevel reference model, group-level effects for new group levels are drawn randomly from a (multivariate) Gaussian distribution. When setting `projpred.mlvl_pred_new` to `TRUE`, all group levels from `newdata` (even those that already exist in the original dataset) are treated as new group levels (if `is.null(newdata)`, all group levels from the original dataset are considered as new group levels in that case).

Value

In the following, N, C_{cat}, and C_{lat} from help topic refmodel-init-get are used. Furthermore, let C denote either C_{cat} (if `type = "response"`) or C_{lat} (if `type = "link"`). Then, if `is.null(ynew)`, the returned object contains the reference model's predictions (with the scale depending on argument `type`) as:

- a length-N vector in case of (i) the traditional projection, (ii) the latent projection with `type = "link"`, or (iii) the latent projection with `type = "response"` and `object$family$cats` being `NULL`;
- an $N \times C$ matrix in case of (i) the augmented-data projection or (ii) the latent projection with `type = "response"` and `object$family$cats` being not `NULL`.

If `!is.null(ynew)`, the returned object is a length-N vector of log posterior predictive densities evaluated at `ynew`.

---

predictor_terms — *Predictor terms used in a* `project()` *run*

Description

For a `projection` object (returned by `project()`, possibly as elements of a `list`), this function extracts the combination of predictor terms onto which the projection was performed.

Usage

```
predictor_terms(object, ...)

## S3 method for class 'projection'
predictor_terms(object, ...)
```

Arguments

object	An object of class projection (returned by project(), possibly as elements of a list) from which to retrieve the predictor terms.
...	Currently ignored.

Value

A character vector of predictor terms.

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Projection onto an arbitrary combination of predictor terms (with a small
# value for `nclusters`, but only for the sake of speed in this example;
# this is not recommended in general):
prj <- project(fit, predictor_terms = c("X1", "X3", "X5"), nclusters = 10,
               seed = 9182)
print(predictor_terms(prj)) # gives `c("X1", "X3", "X5")`
```

---

print.projection *Print information about* project() *output*

Description

This is the print() method for objects of class projection. This method mainly exists to avoid cluttering the console when printing such objects accidentally.

Usage

```
## S3 method for class 'projection'
print(x, ...)
```

Arguments

x	An object of class projection (returned by project(), possibly as elements of a list).
...	Currently ignored.

Value

The input object x (invisible).

---

print.refmodel *Print information about a reference model object*

Description

This is the print() method for reference model objects (objects of class refmodel). This method mainly exists to avoid cluttering the console when printing such objects accidentally.

Usage

```
## S3 method for class 'refmodel'
print(x, ...)
```

Arguments

x	An object of class refmodel (returned by get_refmodel() or init_refmodel()).
...	Currently ignored.

Value

The input object x (invisible).

---

print.vsel *Print results (summary) of a varsel() or cv_varsel() run*

Description

This is the print() method for vsel objects (returned by varsel() or cv_varsel()). It displays a summary of a varsel() or cv_varsel() run by first calling summary.vsel() and then print.vselsummary().

Usage

```
## S3 method for class 'vsel'
print(x, digits = getOption("projpred.digits", 2), ...)
```

Arguments

x	An object of class vsel (returned by varsel() or cv_varsel()).
digits	Passed to argument digits of print.vselsummary().
...	Arguments passed to summary.vsel().

Value

The output of summary.vsel() (invisible).

---

print.vselsummary *Print summary of a varsel() or cv_varsel() run*

Description

This is the print() method for summary objects created by summary.vsel(). It displays a summary of the results from a varsel() or cv_varsel() run.

Usage

```
## S3 method for class 'vselsummary'
print(x, digits = getOption("projpred.digits", 2), ...)
```

Arguments

x	An object of class vselsummary.
digits	Passed to print.data.frame() (for the table containing the submodel performance evaluation results) and print.default() (for the vector containing the reference model performance evaluation results).
...	Arguments passed to print.data.frame() (for the table containing the submodel performance evaluation results) and print.default() (for the vector containing the reference model performance evaluation results).

Details

In the submodel predictive performance table printed at (or towards) the bottom, column ranking_fulldata contains the full-data predictor ranking and column cv_proportions_diag contains the main diagonal of the matrix returned by cv_proportions() (with cumulate as set in the summary.vsel() call that created x). To retrieve the fold-wise predictor rankings, use the ranking() function, possibly followed by cv_proportions() for computing the ranking proportions (which can be visualized by plot.cv_proportions()).

Value

The output of summary.vsel() (invisible).

project *Projection onto submodel(s)*

Description

Project the posterior of the reference model onto the parameter space of a single submodel consisting of a specific combination of predictor terms or (after variable selection) onto the parameter space of a single or multiple submodels of specific sizes.

Usage

```
project(
  object,
  nterms = NULL,
  solution_terms = predictor_terms,
  predictor_terms = NULL,
  refit_prj = TRUE,
  ndraws = 400,
  nclusters = NULL,
  seed = NA,
  verbose = getOption("projpred.verbose", as.integer(interactive())),
  ...
)
```

Arguments

object	An object which can be used as input to get_refmodel() (in particular, objects of class refmodel).
nterms	Only relevant if object is of class vsel (returned by varsel() or cv_varsel()). Ignored if !is.null(predictor_terms). Number of terms for the submodel (the corresponding combination of predictor terms is taken from object). If a numeric vector, then the projection is performed for each element of this vector. If NULL (and is.null(predictor_terms)), then the value suggested by suggest_size() is taken (with default arguments for suggest_size(), implying that this suggested size is based on the ELPD). Note that nterms does not count the intercept, so use nterms = 0 for the intercept-only model.
solution_terms	Deprecated. Please use argument predictor_terms instead.
predictor_terms	If not NULL, then this needs to be a character vector of predictor terms for the submodel onto which the projection will be performed. Argument nterms is ignored in that case. For an object which is not of class vsel, predictor_terms must not be NULL.
refit_prj	A single logical value indicating whether to fit the submodels (again) (TRUE) or—if object is of class vsel—to re-use the submodel fits from the full-data search that was run when creating object (FALSE). For an object which is not of class vsel, refit_prj must be TRUE. See also section "Details" below.

ndraws — Only relevant if refit_prj is TRUE. Number of posterior draws to be projected. Ignored if nclusters is not NULL or if the reference model is of class datafit (in which case one cluster is used). If both (nclusters and ndraws) are NULL, the number of posterior draws from the reference model is used for ndraws. See also section "Details" below.

nclusters — Only relevant if refit_prj is TRUE. Number of clusters of posterior draws to be projected. Ignored if the reference model is of class datafit (in which case one cluster is used). For the meaning of NULL, see argument ndraws. See also section "Details" below.

seed — Pseudorandom number generation (PRNG) seed by which the same results can be obtained again if needed. Passed to argument seed of set.seed(), but can also be NA to not call set.seed() at all. If not NA, then the PRNG state is reset (to the state before calling project()) upon exiting project(). Here, seed is used for clustering the reference model's posterior draws (if !is.null(nclusters)) and for drawing new group-level effects when predicting from a multilevel submodel (however, not yet in case of a GAMM) and having global option projpred.mlvl_pred_new set to TRUE. (Such a prediction takes place when calculating output elements dis and ce.)

verbose — A single integer value from the set $\{0, 1, 2\}$ (if !is.null(predictor_terms), 1 and 2 have the same effect), indicating how much information (if any) to print out during the computations. Higher values indicate that more information should be printed, 0 deactivates the verbose mode. Internally, argument verbose is coerced to integer via as.integer(), so technically, a single logical value or a single numeric value work as well.

... — Arguments passed to get_refmodel() (if get_refmodel() is actually used; see argument object) as well as to the divergence minimizer (if refit_prj is TRUE).

Details

Arguments ndraws and nclusters are automatically truncated at the number of posterior draws in the reference model (which is 1 for datafits). Using less draws or clusters in ndraws or nclusters than posterior draws in the reference model may result in slightly inaccurate projection performance. Increasing these arguments affects the computation time linearly.

If refit_prj = FALSE (which is only possible if object is of class vsel), project() retrieves the submodel fits from the full-data search that was run when creating object. Usually, the search relies on a rather coarse clustering or thinning of the reference model's posterior draws (by default, varsel() and cv_varsel() use nclusters = 20). Consequently, project() with refit_prj = FALSE then inherits this coarse clustering or thinning.

Value

If the projection is performed onto a single submodel (i.e., length(nterms) == 1 || !is.null(predictor_terms)), an object of class projection which is a list containing the following elements:

dis Projected draws for the dispersion parameter.

ce The cross-entropy part of the Kullback-Leibler (KL) divergence from the reference model to the submodel. For some families, this is not the actual cross-entropy, but a reduced one where terms which would cancel out when calculating the KL divergence have been dropped. In case of the Gaussian family, that reduced cross-entropy is further modified, yielding merely a proxy.

wdraws_prj Weights for the projected draws.

predictor_terms A character vector of the submodel's predictor terms.

outdmin A list containing the submodel fits (one fit per projected draw). This is the same as the return value of the div_minimizer function (see init_refmodel()), except if project() was used with an object of class vsel based on an L1 search as well as with refit_prj = FALSE, in which case this is the output from an internal *L1-penalized* divergence minimizer.

cl_ref A numeric vector of length equal to the number of posterior draws in the reference model, containing the cluster indices of these draws.

wdraws_ref A numeric vector of length equal to the number of posterior draws in the reference model, giving the weights of these draws. These weights should be treated as not being normalized (i.e., they don't necessarily sum to 1).

const_wdraws_prj A single logical value indicating whether the projected draws have constant weights (TRUE) or not (FALSE).

refmodel The reference model object.

If the projection is performed onto more than one submodel, the output from above is returned for each submodel, giving a list with one element for each submodel.

The elements of an object of class projection are not meant to be accessed directly but instead via helper functions (see the main vignette and projpred-package; see also as_draws_matrix.projection(), argument return_draws_matrix of proj_linpred(), and argument nresample_clusters of proj_predict() for the intended use of the weights stored in element wdraws_prj).

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Run varsel() (here without cross-validation, with L1 search, and with small
# values for `nterms_max` and `nclusters_pred`, but only for the sake of
# speed in this example; this is not recommended in general):
vs <- varsel(fit, method = "L1", nterms_max = 3, nclusters_pred = 10,
             seed = 5555)

# Projection onto the best submodel with 2 predictor terms (with a small
# value for `nclusters`, but only for the sake of speed in this example;
```

```
# this is not recommended in general):
prj_from_vs <- project(vs, nterms = 2, nclusters = 10, seed = 9182)

# Projection onto an arbitrary combination of predictor terms (with a small
# value for `nclusters`, but only for the sake of speed in this example;
# this is not recommended in general):
prj <- project(fit, predictor_terms = c("X1", "X3", "X5"), nclusters = 10,
               seed = 9182)
```

`ranking` *Predictor ranking(s)*

Description

Extracts the *predictor ranking(s)* from an object of class `vsel` (returned by `varsel()` or `cv_varsel()`). A predictor ranking is simply a character vector of predictor terms ranked by predictive relevance (with the most relevant term first). In any case, objects of class `vsel` contain the predictor ranking based on the *full-data* search. If an object of class `vsel` is based on a cross-validation (CV) with fold-wise searches (i.e., if it was created by `cv_varsel()` with `validate_search = TRUE`), then it also contains *fold-wise* predictor rankings.

Usage

```
ranking(object, ...)

## S3 method for class 'vsel'
ranking(object, nterms_max = NULL, ...)
```

Arguments

`object`	The object from which to retrieve the predictor ranking(s). Possible classes may be inferred from the names of the corresponding methods (see also the description).
`...`	Currently ignored.
`nterms_max`	Maximum submodel size (number of predictor terms) for the predictor ranking(s), i.e., the submodel size at which to cut off the predictor ranking(s). Using `NULL` is effectively the same as setting `nterms_max` to the full model size, i.e., this means to not cut off the predictor ranking(s) at all. Note that `nterms_max` does not count the intercept, so `nterms_max = 1` corresponds to the submodel consisting of the first (non-intercept) predictor term.

Value

An object of class `ranking` which is a `list` with the following elements:

- `fulldata`: The predictor ranking from the full-data search.

- `foldwise`: The predictor rankings from the fold-wise searches in the form of a character matrix (only available if `object` is based on a CV with fold-wise searches, otherwise element `foldwise` is `NULL`). The rows of this matrix correspond to the CV folds and the columns to the submodel sizes. Each row contains the predictor ranking from the search of that CV fold.

See Also

`cv_proportions()`

Examples

```
# For an example, see `?plot.cv_proportions`.
```

`refmodel-init-get` *Reference model and more general information*

Description

Function `get_refmodel()` is a generic function whose methods usually call `init_refmodel()` which is the underlying workhorse (and may also be used directly without a call to `get_refmodel()`).

Both, `get_refmodel()` and `init_refmodel()`, create an object containing information needed for the projection predictive variable selection, namely about the reference model, the submodels, and how the projection should be carried out. For the sake of simplicity, the documentation may refer to the resulting object also as "reference model" or "reference model object", even though it also contains information about the submodels and the projection.

A "typical" reference model object is created by `get_refmodel.stanreg()` and `brms::get_refmodel.brmsfit()`, either implicitly by a call to a top-level function such as `project()`, `varsel()`, and `cv_varsel()` or explicitly by a call to `get_refmodel()`. All non-"typical" reference model objects will be called "custom" reference model objects.

Some arguments are for K-fold cross-validation (K-fold CV) only; see `cv_varsel()` for the use of K-fold CV in **projpred**.

Usage

```
get_refmodel(object, ...)

## S3 method for class 'refmodel'
get_refmodel(object, ...)

## S3 method for class 'vsel'
get_refmodel(object, ...)

## S3 method for class 'projection'
get_refmodel(object, ...)

## Default S3 method:
```

```
get_refmodel(object, family = NULL, ...)

## S3 method for class 'stanreg'
get_refmodel(object, latent = FALSE, dis = NULL, ...)

init_refmodel(
  object,
  data,
  formula,
  family,
  ref_predfun = NULL,
  div_minimizer = NULL,
  proj_predfun = NULL,
  extract_model_data = NULL,
  cvfun = NULL,
  cvfits = NULL,
  dis = NULL,
  cvrefbuilder = NULL,
  called_from_cvrefbuilder = FALSE,
  ...
)
```

Arguments

object	For `init_refmodel()`, an object that the functions from arguments `extract_model_data` and `ref_predfun` can be applied to, with a `NULL` object being treated specially (see section "Value" below). For `get_refmodel.default()`, an object that function `family()` can be applied to in order to retrieve the family (if argument `family` is `NULL`), additionally to the properties required for `init_refmodel()`. For non-default methods of `get_refmodel()`, an object of the corresponding class.
...	For `get_refmodel.default()` and `get_refmodel.stanreg()`: arguments passed to `init_refmodel()`. For the `get_refmodel()` generic: arguments passed to the appropriate method. For `init_refmodel()`: arguments passed to `extend_family()` (apart from `family`).
family	An object of class `family` representing the observation model (i.e., the distributional family for the response) of the *submodels*. (However, the link and the inverse-link function of this `family` are also used for quantities like predictions and fitted values related to the *reference model*.) May be `NULL` for `get_refmodel.default()` in which case the family is retrieved from `object`. For custom reference models, `family` does not have to coincide with the family of the reference model (if the reference model possesses a formal `family` at all). In typical reference models, however, these families do coincide. Furthermore, the latent projection is an exception where `family` is not the family of the submodels (in that case, the family of the submodels is the `gaussian()` family).
latent	A single logical value indicating whether to use the latent projection (`TRUE`) or not (`FALSE`). Note that setting `latent = TRUE` causes all arguments starting with `augdat_` to be ignored.

`dis` A vector of posterior draws for the reference model's dispersion parameter or—more precisely—the posterior values for the reference model's parameter-conditional predictive variance (assuming that this variance is the same for all observations). May be `NULL` if the submodels have no dispersion parameter or if the submodels do have a dispersion parameter, but `object` is `NULL` (in which case `0` is used for `dis`). Note that for the `gaussian()` `family`, `dis` is the standard deviation, not the variance.

`data` A `data.frame` containing the data to use for the projection predictive variable selection. Any `contrasts` attributes of the dataset's columns are silently removed. For custom reference models, the columns of `data` do not necessarily have to coincide with those of the dataset used for fitting the reference model, but keep in mind that a row-subset of `data` is used for argument `newdata` of `ref_predfun` during K-fold CV.

`formula` The full formula to use for the search procedure. For custom reference models, this does not necessarily coincide with the reference model's formula. For general information about formulas in R, see `formula`. For information about possible right-hand side (i.e., predictor) terms in `formula` here, see the main vignette and section "Formula terms" below. For multilevel formulas, see also package **lme4** (in particular, functions `lme4::lmer()` and `lme4::glmer()`). For additive formulas, see also packages **mgcv** (in particular, function `mgcv::gam()`) and **gamm4** (in particular, function `gamm4::gamm4()`).

`ref_predfun` Prediction function for the linear predictor of the reference model, including offsets (if existing). See also section "Arguments `ref_predfun`, `proj_predfun`, and `div_minimizer`" below. If `object` is `NULL`, `ref_predfun` is ignored and an internal default is used instead.

`div_minimizer` A function for minimizing the Kullback-Leibler (KL) divergence from the reference model to a submodel (i.e., for performing the projection of the reference model onto a submodel). The output of `div_minimizer` is used, e.g., by `proj_predfun`'s argument `fits`. See also section "Arguments `ref_predfun`, `proj_predfun`, and `div_minimizer`" below.

`proj_predfun` Prediction function for the linear predictor of a submodel onto which the reference model is projected. See also section "Arguments `ref_predfun`, `proj_predfun`, and `div_minimizer`" below.

`extract_model_data` A function for fetching some variables (response, observation weights, offsets) from the original dataset (supplied to argument `data`) or from a new dataset. May be `NULL` for using an internal default that essentially corresponds to `y_wobs_offs()`. See also section "Argument `extract_model_data`" below.

`cvfun` For K-fold CV only. A function that, given a fold indices vector, fits the reference model separately for each fold and returns the K model fits as a `list`. If `object` is `NULL`, `cvfun` may be `NULL` for using an internal default. Only one of `cvfits` and `cvfun` needs to be provided (for K-fold CV). Note that `cvfits` takes precedence over `cvfun`, i.e., if both are provided, `cvfits` is used.

`cvfits` For K-fold CV only. A `list` containing the K reference model refits from which reference model objects are created. This `list` needs to have an attribute called `folds`, consisting of an integer vector giving the fold indices (one fold

index per observation). Only one of `cvfits` and `cvfun` needs to be provided (for K-fold CV). Note that `cvfits` takes precedence over `cvfun`, i.e., if both are provided, `cvfits` is used.

`cvrefbuilder` For K-fold CV only. A function that, given a reference model fit for fold $k \in \{1, ..., K\}$, returns an object of the same type as `init_refmodel()` does. The reference model fit for fold k is the k-th element of the return value of `cvfun` or the k-th element of the `list` supplied to `cvfits` (either here in `init_refmodel()` or in `cv_varsel.refmodel()`), extended by elements `omitted` (containing the indices of the left-out observations in that fold) and `projpred_k` (containing the integer k) if that k-th element is a `list` itself (otherwise, `omitted` and `projpred_k` are appended as attributes). Argument `cvrefbuilder` may be `NULL` for using an internal default: `get_refmodel()` if `object` is not `NULL` and a function calling `init_refmodel()` appropriately (with the assumption `dis = 0`) if `object` is `NULL`.

`called_from_cvrefbuilder`
A single logical value indicating whether `init_refmodel()` is called from a `cvrefbuilder` function (`TRUE`) or not (`FALSE`). Currently, `TRUE` only causes some warnings to be suppressed (warnings which don't need to be thrown for each of the K reference model objects because it is sufficient to throw them for the original reference model object only). This argument is mainly for internal use, but may also be helpful for users with a custom `cvrefbuilder` function.

Value

An object that can be passed to all the functions that take the reference model fit as the first argument, such as `varsel()`, `cv_varsel()`, `project()`, `proj_linpred()`, and `proj_predict()`. Usually, the returned object is of class `refmodel`. However, if `object` is `NULL`, the returned object is of class `datafit` as well as of class `refmodel` (with `datafit` being first). Objects of class `datafit` are handled differently at several places throughout this package.

The elements of the returned object are not meant to be accessed directly but instead via downstream functions (see the functions mentioned above as well as `predict.refmodel()`).

Formula terms

Although bad practice (in general), a reference model lacking an intercept can be used within **projpred**. However, it will always be projected onto submodels which *include* an intercept. The reason is that even if the true intercept in the reference model is zero, this does not need to hold for the submodels.

In multilevel (group-level) terms, function calls on the right-hand side of the `|` character (e.g., `(1 | gr(group_variable))`, which is possible in **brms**) are currently not allowed in **projpred**.

For additive models (still an experimental feature), only `mgcv::s()` and `mgcv::t2()` are currently supported as smooth terms. Furthermore, these need to be called without any arguments apart from the predictor names (symbols). For example, for smoothing the effect of a predictor `x`, only `s(x)` or `t2(x)` are allowed. As another example, for smoothing the joint effect of two predictors `x` and `z`, only `s(x, z)` or `t2(x, z)` are allowed (and analogously for higher-order joint effects, e.g., of three predictors). Note that all smooth terms need to be included in `formula` (there is no `random` argument as in `rstanarm::stan_gamm4()`, for example).

Arguments `ref_predfun`**,** `proj_predfun`**, and** `div_minimizer`

Arguments `ref_predfun`, `proj_predfun`, and `div_minimizer` may be `NULL` for using an internal default (see projpred-package for the functions used by the default divergence minimizers). Otherwise, let N denote the number of observations (in case of CV, these may be reduced to each fold), S_{ref} the number of posterior draws for the reference model's parameters, and S_{prj} the number of draws for the parameters of a submodel that the reference model has been projected onto (short: the number of projected draws). For the augmented-data projection, let C_{cat} denote the number of response categories, C_{lat} the number of latent response categories (which typically equals $C_{\text{cat}} - 1$), and define $N_{\text{augcat}} := N \cdot C_{\text{cat}}$ as well as $N_{\text{auglat}} := N \cdot C_{\text{lat}}$. Then the functions supplied to these arguments need to have the following prototypes:

- `ref_predfun`: `ref_predfun(fit, newdata = NULL)` where:
  - `fit` accepts the reference model fit as given in argument `object` (but possibly refitted to a subset of the observations, as done in K-fold CV).
  - `newdata` accepts either `NULL` (for using the original dataset, typically stored in `fit`) or data for new observations (at least in the form of a `data.frame`).
- `proj_predfun`: `proj_predfun(fits, newdata)` where:
  - `fits` accepts a `list` of length S_{prj} containing this number of submodel fits. This `list` is the same as that returned by `project()` in its output element `outdmin` (which in turn is the same as the return value of `div_minimizer`, except if `project()` was used with an `object` of class `vsel` based on an L1 search as well as with `refit_prj = FALSE`).
  - `newdata` accepts data for new observations (at least in the form of a `data.frame`).
- `div_minimizer` does not need to have a specific prototype, but it needs to be able to be called with the following arguments:
  - `formula` accepts either a standard `formula` with a single response (if $S_{\text{prj}} = 1$ or in case of the augmented-data projection) or a `formula` with $S_{\text{prj}} > 1$ response variables `cbind()`-ed on the left-hand side in which case the projection has to be performed for each of the response variables separately.
  - `data` accepts a `data.frame` to be used for the projection. In case of the traditional or the latent projection, this dataset has N rows. In case of the augmented-data projection, this dataset has N_{augcat} rows.
  - `family` accepts an object of class `family`.
  - `weights` accepts either observation weights (at least in the form of a numeric vector) or `NULL` (for using a vector of ones as weights).
  - `projpred_var` accepts an $N \times S_{\text{prj}}$ matrix of predictive variances (necessary for **projpred**'s internal GLM fitter) in case of the traditional or the latent projection and an $N_{\text{augcat}} \times S_{\text{prj}}$ matrix (containing only `NA`s) in case of the augmented-data projection.
  - `projpred_ws_aug` accepts an $N \times S_{\text{prj}}$ matrix of expected values for the response in case of the traditional or the latent projection and an $N_{\text{augcat}} \times S_{\text{prj}}$ matrix of probabilities for the response categories in case of the augmented-data projection.
  - `...` accepts further arguments specified by the user (or by **projpred**).

The return value of these functions needs to be:

- `ref_predfun`: for the traditional or the latent projection, an $N \times S_{\text{ref}}$ matrix; for the augmented-data projection, an $S_{\text{ref}} \times N \times C_{\text{lat}}$ array (the only exception is the augmented-data projection

for the binomial() family in which case ref_predfun needs to return an $N \times S_{\text{ref}}$ matrix just like for the traditional projection because the array is constructed by an internal wrapper function).

- proj_predfun: for the traditional or the latent projection, an $N \times S_{\text{prj}}$ matrix; for the augmented-data projection, an $N \times C_{\text{lat}} \times S_{\text{prj}}$ array.
- div_minimizer: a list of length S_{prj} containing this number of submodel fits.

Argument extract_model_data

The function supplied to argument extract_model_data needs to have the prototype

```
extract_model_data(object, newdata, wrhs = NULL, orhs = NULL,
                   extract_y = TRUE)
```

where:

- object accepts the reference model fit as given in argument object (but possibly refitted to a subset of the observations, as done in K-fold CV).
- newdata accepts data for new observations (at least in the form of a data.frame).
- wrhs accepts at least (i) a right-hand side formula consisting only of the variable in newdata containing the observation weights or (ii) NULL for using the observation weights corresponding to newdata (typically, the observation weights are stored in a column of newdata; if the model was fitted without observation weights, a vector of ones should be used).
- orhs accepts at least (i) a right-hand side formula consisting only of the variable in newdata containing the offsets or (ii) NULL for using the offsets corresponding to newdata (typically, the offsets are stored in a column of newdata; if the model was fitted without offsets, a vector of zeros should be used).
- extract_y accepts a single logical value indicating whether output element y (see below) shall be NULL (TRUE) or not (FALSE).

The return value of extract_model_data needs to be a list with elements y, weights, and offset, each being a numeric vector containing the data for the response, the observation weights, and the offsets, respectively. An exception is that y may also be NULL (depending on argument extract_y), a non-numeric vector, or a factor.

The weights and offsets returned by extract_model_data will be assumed to hold for the reference model as well as for the submodels.

Above, arguments wrhs and orhs were assumed to have defaults of NULL. It should be possible to use defaults other than NULL, but we strongly recommend to use NULL. If defaults other than NULL are used, they need to imply the behaviors described at items "(ii)" (see the descriptions of wrhs and orhs).

Augmented-data projection

If a custom reference model for an augmented-data projection is needed, see also extend_family().

For the augmented-data projection, the response vector resulting from extract_model_data is internally coerced to a factor (using as.factor()). The levels of this factor have to be identical

to family$cats (*after* applying extend_family() internally; see extend_family()'s argument augdat_y_unqs).

Note that response-specific offsets (i.e., one length-N offset vector per response category) are not supported by **projpred** yet. So far, only offsets which are the same across all response categories are supported. This is why in case of the brms::categorical() family, offsets are currently not supported at all.

Currently, object = NULL (i.e., a datafit; see section "Value") is not supported in case of the augmented-data projection.

Latent projection

If a custom reference model for a latent projection is needed, see also extend_family().

For the latent projection, family$cats (*after* applying extend_family() internally; see extend_family()'s argument latent_y_unqs) currently must not be NULL if the original (i.e., non-latent) response is a factor. Conversely, if family$cats (*after* applying extend_family()) is non-NULL, the response vector resulting from extract_model_data is internally coerced to a factor (using as.factor()). The levels of this factor have to be identical to that non-NULL element family$cats.

Currently, object = NULL (i.e., a datafit; see section "Value") is not supported in case of the latent projection.

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Define the reference model object explicitly:
ref <- get_refmodel(fit)
print(class(ref)) # gives `"refmodel"`
# Now see, for example, `?varsel`, `?cv_varsel`, and `?project` for
# possible post-processing functions. Most of the post-processing functions
# call get_refmodel() internally at the beginning, so you will rarely need
# to call get_refmodel() yourself.

# A custom reference model object which may be used in a variable selection
# where the candidate predictors are not a subset of those used for the
# reference model's predictions:
ref_cust <- init_refmodel(
  fit,
  data = dat_gauss,
  formula = y ~ X6 + X7,
  family = gaussian(),
  cvfun = function(folds) {
```

```
    kfold(
      fit, K = max(folds), save_fits = TRUE, folds = folds, cores = 1
    )$fits[, "fit"]
  },
  dis = as.matrix(fit)[, "sigma"],
  cvrefbuilder = function(cvfit) {
    init_refmodel(cvfit,
                  data = dat_gauss[-cvfit$omitted, , drop = FALSE],
                  formula = y ~ X6 + X7,
                  family = gaussian(),
                  dis = as.matrix(cvfit)[, "sigma"],
                  called_from_cvrefbuilder = TRUE)
  }
)
# Now, the post-processing functions mentioned above (for example,
# varsel(), cv_varsel(), and project()) may be applied to `ref_cust`.
```

`run_cvfun` *Create* `cvfits` *from* `cvfun`

Description

A helper function that can be used to create input for `cv_varsel.refmodel()`'s argument `cvfits` by running first `cv_folds()` and then the reference model object's `cvfun` (see `init_refmodel()`). This is helpful if K-fold CV is run multiple times based on the same K reference model refits.

Usage

```
run_cvfun(object, ...)

## Default S3 method:
run_cvfun(object, ...)

## S3 method for class 'refmodel'
run_cvfun(
  object,
  K = if (!inherits(object, "datafit")) 5 else 10,
  folds = NULL,
  seed = NA,
  ...
)
```

Arguments

`object`	An object of class `refmodel` (returned by `get_refmodel()` or `init_refmodel()`) or an object that can be passed to argument `object` of `get_refmodel()`.
`...`	For `run_cvfun.default()`: Arguments passed to `get_refmodel()`. For `run_cvfun.refmodel()`: Currently ignored.

K	Number of folds. Must be at least 2 and not exceed the number of observations. Ignored if folds is not NULL.
folds	Either NULL for determining the CV folds automatically via cv_folds() (using argument K) or a numeric (in fact, integer) vector giving the fold index for each observation. In the latter case, argument K is ignored.
seed	Pseudorandom number generation (PRNG) seed by which the same results can be obtained again if needed. Passed to argument seed of set.seed(), but can also be NA to not call set.seed() at all. If not NA, then the PRNG state is reset (to the state before calling run_cvfun()) upon exiting run_cvfun().

Value

An object that can be used as input for cv_varsel.refmodel()'s argument cvfits.

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Define the reference model object explicitly (not really necessary here
# because the get_refmodel() call is quite fast in this example, but in
# general, this approach is faster than defining the reference model object
# multiple times implicitly):
ref <- get_refmodel(fit)

# Run the reference model object's `cvfun` (with a small value for `K`, but
# only for the sake of speed in this example; this is not recommended in
# general):
cv_fits <- run_cvfun(ref, K = 2, seed = 184)

# Run cv_varsel() (with L1 search and small values for `nterms_max` and
# `nclusters_pred`, but only for the sake of speed in this example; this is
# not recommended in general) and use `cv_fits` there:
cvvs_L1 <- cv_varsel(ref, method = "L1", cv_method = "kfold",
                     cvfits = cv_fits, nterms_max = 3, nclusters_pred = 10,
                     seed = 5555)
# Now see, for example, `?print.vsel`, `?plot.vsel`, `?suggest_size.vsel`,
# and `?ranking` for possible post-processing functions.

# The purpose of run_cvfun() is to create an object that can be used in
# multiple cv_varsel() calls, e.g., to check the sensitivity to the search
# method (L1 or forward):
cvvs_fw <- cv_varsel(ref, method = "forward", cv_method = "kfold",
```

```
                    cvfits = cv_fits, nterms_max = 3, nclusters = 5,
                    nclusters_pred = 10, seed = 5555)

# Stratified K-fold CV is straightforward:
n_strat <- 3L
set.seed(692)
# Some example strata:
strat_fac <- sample(paste0("lvl", seq_len(n_strat)), size = nrow(dat_gauss),
                    replace = TRUE,
                    prob = diff(c(0, pnorm(seq_len(n_strat - 1L) - 0.5), 1)))
table(strat_fac)
# Use loo::kfold_split_stratified() to create the folds vector:
folds_strat <- loo::kfold_split_stratified(K = 2, x = strat_fac)
table(folds_strat, strat_fac)
# Call run_cvfun(), but this time with argument `folds` instead of `K` (here,
# specifying argument `seed` would not be necessary because of the set.seed()
# call above, but we specify it nonetheless for the sake of generality):
cv_fits_strat <- run_cvfun(ref, folds = folds_strat, seed = 391)
# Now use `cv_fits_strat` analogously to `cv_fits` from above.
```

`solution_terms` *Retrieve the full-data solution path from a* `varsel()` *or* `cv_varsel()` *run or the predictor combination from a* `project()` *run*

Description

The `solution_terms.vsel()` method retrieves the solution path from a full-data search (`vsel` objects are returned by `varsel()` or `cv_varsel()`). The `solution_terms.projection()` method retrieves the predictor combination onto which a projection was performed (`projection` objects are returned by `project()`, possibly as elements of a `list`). Both methods (and hence also the `solution_terms()` generic) are deprecated and will be removed in a future release. Please use `ranking()` instead of `solution_terms.vsel()` (`ranking()`'s output element `fulldata` contains the full-data predictor ranking that is extracted by `solution_terms.vsel()`; `ranking()`'s output element `foldwise` contains the fold-wise predictor rankings—if available—which were previously not accessible via a built-in function) and `predictor_terms()` instead of `solution_terms.projection()`.

Usage

```
solution_terms(object, ...)

## S3 method for class 'vsel'
solution_terms(object, ...)

## S3 method for class 'projection'
solution_terms(object, ...)
```

Arguments

object	The object from which to retrieve the predictor terms. Possible classes may be inferred from the names of the corresponding methods (see also the description).
...	Currently ignored.

Value

A character vector of predictor terms.

---

suggest_size *Suggest submodel size*

Description

This function can suggest an appropriate submodel size based on a decision rule described in section "Details" below. Note that this decision is quite heuristic and should be interpreted with caution. It is recommended to examine the results via `plot.vsel()`, `cv_proportions()`, `plot.cv_proportions()`, and/or `summary.vsel()` and to make the final decision based on what is most appropriate for the problem at hand.

Usage

```
suggest_size(object, ...)

## S3 method for class 'vsel'
suggest_size(
  object,
  stat = "elpd",
  pct = 0,
  type = "upper",
  thres_elpd = NA,
  warnings = TRUE,
  ...
)
```

Arguments

object	An object of class `vsel` (returned by `varsel()` or `cv_varsel()`).
...	Arguments passed to `summary.vsel()`, except for `object`, `stats` (which is set to `stat`), `type`, and `deltas` (which is set to `TRUE`). See section "Details" below for some important arguments which may be passed here.
stat	Performance statistic (i.e., utility or loss) used for the decision. See argument `stats` of `summary.vsel()` and `plot.vsel()` for possible choices.
pct	A number giving the proportion (*not* percents) of the *relative* null model utility one is willing to sacrifice. See section "Details" below for more information.

type	Either "upper" or "lower" determining whether the decision is based on the upper or lower uncertainty interval bound, respectively. See section "Details" below for more information.
thres_elpd	Only relevant if stat %in% c("elpd", "mlpd", "gmpd")). The threshold for the ELPD difference (taking the submodel's ELPD minus the baseline model's ELPD) above which the submodel's ELPD is considered to be close enough to the baseline model's ELPD. An equivalent rule is applied in case of the MLPD and the GMPD. See section "Details" for a formalization. Supplying NA deactivates this.
warnings	Mainly for internal use. A single logical value indicating whether to throw warnings if automatic suggestion fails. Usually there is no reason to set this to FALSE.

Details

In general (beware of special cases below), the suggested model size is the smallest model size $j \in \{0, 1, ..., \texttt{nterms_max}\}$ for which either the lower or upper bound (depending on argument type) of the uncertainty interval (with nominal coverage 1 - alpha; see argument alpha of summary.vsel()) for $U_j - U_{\text{base}}$ (with U_j denoting the j-th submodel's true utility and U_{base} denoting the baseline model's true utility) falls above (or is equal to)

$$\texttt{pct} \cdot (u_0 - u_{\text{base}})$$

where u_0 denotes the null model's estimated utility and u_{base} the baseline model's estimated utility. The baseline model is either the reference model or the best submodel found (see argument baseline of summary.vsel()).

In doing so, loss statistics like the root mean squared error (RMSE) and the mean squared error (MSE) are converted to utilities by multiplying them by -1, so a call such as suggest_size(object, stat = "rmse", type = "upper") finds the smallest model size whose upper uncertainty interval bound for the *negative* RMSE or MSE exceeds (or is equal to) the cutoff (or, equivalently, has the lower uncertainty interval bound for the RMSE or MSE below—or equal to—the cutoff). This is done to make the interpretation of argument type the same regardless of argument stat.

For the geometric mean predictive density (GMPD), the decision rule above is applied on log() scale. In other words, if the true GMPD is denoted by U_j^* for the j-th submodel and U_{base}^* for the baseline model (so that U_j and U_{base} from above are given by $U_j = \log(U_j^*)$ and $U_{\text{base}} = \log(U_{\text{base}}^*)$), then suggest_size() yields the smallest model size whose lower or upper (depending on argument type) uncertainty interval bound for $\frac{U_j^*}{U_{\text{base}}^*}$ exceeds (or is equal to)

$$(\frac{u_0^*}{u_{\text{base}}^*})^{\texttt{pct}}$$

where u_0^* denotes the null model's estimated GMPD and u_{base}^* the baseline model's estimated GMPD.

If !is.na(thres_elpd) and stat = "elpd", the decision rule above is extended: The suggested model size is then the smallest model size j fulfilling the rule above *or* $u_j - u_{\text{base}} > \texttt{thres_elpd}$. Correspondingly, in case of stat = "mlpd" (and !is.na(thres_elpd)), the suggested model size is the smallest model size j fulfilling the rule above *or* $u_j - u_{\text{base}} > \frac{\texttt{thres_elpd}}{N}$ with N denoting the number of observations. Correspondingly, in case of stat = "gmpd" (and !is.na(thres_elpd)), the suggested model size is the smallest model size j fulfilling the rule above *or* $\frac{u_j^*}{u_{\text{base}}^*} > \exp(\frac{\texttt{thres_elpd}}{N})$.

For example (disregarding the special extensions in case of `!is.na(thres_elpd)` with `stat %in% c("elpd", "mlpd", "gmpd")`), `alpha = 2 * pnorm(-1)`, `pct = 0`, and `type = "upper"` means that we select the smallest model size for which the upper bound of the `1 - 2 * pnorm(-1)` (approximately 68.3 %) uncertainty interval for $U_j - U_{\text{base}}$ ($\frac{U_j^*}{U_{\text{base}}^*}$ in case of the GMPD) exceeds (or is equal to) zero (one in case of the GMPD), that is (if `stat` is a performance statistic for which a normal-approximation uncertainty interval is used, see argument `stats` of `summary.vsel()` and `plot.vsel()`), for which the submodel's utility estimate is at most one standard error smaller than the baseline model's utility estimate (with that standard error referring to the utility *difference*).

Apart from the two `summary.vsel()` arguments mentioned above (`alpha` and `baseline`), `resp_oscale` is another important `summary.vsel()` argument that may be passed via `...`.

Value

A single numeric value, giving the suggested submodel size (or `NA` if the suggestion failed).

The intercept is not counted by `suggest_size()`, so a suggested size of zero stands for the intercept-only model.

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Run varsel() (here without cross-validation, with L1 search, and with small
# values for `nterms_max` and `nclusters_pred`, but only for the sake of
# speed in this example; this is not recommended in general):
vs <- varsel(fit, method = "L1", nterms_max = 3, nclusters_pred = 10,
             seed = 5555)
print(suggest_size(vs))
```

---

summary.vsel *Summary of a* `varsel()` *or* `cv_varsel()` *run*

Description

This is the `summary()` method for `vsel` objects (returned by `varsel()` or `cv_varsel()`). Apart from some general information about the `varsel()` or `cv_varsel()` run, it shows the full-data predictor ranking, basic information about the (CV) variability in the ranking of the predictors (if available; inferred from `cv_proportions()`), and estimates for user-specified predictive performance statistics. For a graphical representation, see `plot.vsel()`. For extracting the predictive

performance results printed at the bottom of the output created by this summary() method, see performances().

Usage

```
## S3 method for class 'vsel'
summary(
  object,
  nterms_max = NULL,
  stats = "elpd",
  type = c("mean", "se", "diff", "diff.se"),
  deltas = FALSE,
  alpha = 2 * pnorm(-1),
  baseline = if (!inherits(object$refmodel, "datafit")) "ref" else "best",
  resp_oscale = TRUE,
  cumulate = FALSE,
  ...
)
```

Arguments

object	An object of class vsel (returned by varsel() or cv_varsel()).
nterms_max	Maximum submodel size (number of predictor terms) for which the performance statistics are calculated. Using NULL is effectively the same as length(ranking(object)$fulldata). Note that nterms_max does not count the intercept, so use nterms_max = 0 for the intercept-only model. For plot.vsel(), nterms_max must be at least 1.
stats	One or more character strings determining which performance statistics (i.e., utilities or losses) to estimate based on the observations in the evaluation (or "test") set (in case of cross-validation, these are all observations because they are partitioned into multiple test sets; in case of varsel() with d_test = NULL, these are again all observations because the test set is the same as the training set). Available statistics are: • "elpd": expected log (pointwise) predictive density (for a new dataset) (ELPD). Estimated by the sum of the observation-specific log predictive density values (with each of these predictive density values being a—possibly weighted—average across the parameter draws). For the corresponding uncertainty interval, a normal approximation is used. • "mlpd": mean log predictive density (MLPD), that is, the ELPD divided by the number of observations. For the corresponding uncertainty interval, a normal approximation is used. • "gmpd": geometric mean predictive density (GMPD), that is, exp() of the MLPD. The GMPD is especially helpful for discrete response families (because there, the GMPD is bounded by zero and one). For the corresponding standard error, the delta method is used. The corresponding uncertainty interval type is "exponentiated normal approximation" because the uncertainty interval bounds are the exponentiated uncertainty interval bounds of the MLPD.

- "mse": mean squared error (only available in the situations mentioned in section "Details" below). For the corresponding uncertainty interval, a log-normal approximation is used if deltas is FALSE and a normal approximation is used if deltas is TRUE (or "mixed", in case of plot.vsel()).
- "rmse": root mean squared error (only available in the situations mentioned in section "Details" below). For the corresponding standard error, the delta method is used. For the corresponding uncertainty interval, a log-normal approximation is used if deltas is FALSE and a normal approximation is used if deltas is TRUE (or "mixed", in case of plot.vsel()).
- "R2": R-squared, i.e., coefficient of determination (only available in the situations mentioned in section "Details" below). For the corresponding standard error, the delta method is used. For the corresponding uncertainty interval, a normal approximation is used.
- "acc" (or its alias, "pctcorr"): classification accuracy (only available in the situations mentioned in section "Details" below). By "classification accuracy", we mean the proportion of correctly classified observations. For this, the response category ("class") with highest probability (the probabilities are model-based) is taken as the prediction ("classification") for an observation. For the corresponding uncertainty interval, a normal approximation is used.
- "auc": area under the ROC curve (only available in the situations mentioned in section "Details" below). For the corresponding standard error and lower and upper uncertainty interval bounds, bootstrapping is used. Not supported in case of subsampled LOO-CV (see argument nloo of cv_varsel()).

type — One or more items from "mean", "se", "lower", "upper", "diff", "diff.lower", "diff.upper", and "diff.se" indicating which of these to compute for each item from stats (mean, standard error, lower and upper uncertainty interval bounds, mean difference to the corresponding statistic of the reference model, lower and upper uncertainty interval bound for this difference, and standard error of this difference, respectively; note that for the GMPD, "diff", "diff.lower", "diff.upper", and "diff.se" actually refer to the ratio vs. the reference model, not the difference). The uncertainty interval bounds belong to uncertainty intervals with (nominal) coverage 1 - alpha. Items "diff", "diff.lower", "diff.upper", and "diff.se" are only supported if deltas is FALSE.

deltas — May be set to FALSE or TRUE. If FALSE, the submodel performance statistics are estimated on their actual scale. If TRUE, the submodel statistics are estimated relatively to the baseline model (see argument baseline). For the GMPD, the term "relatively" refers to the *ratio* vs. the baseline model (i.e., the submodel statistic divided by the baseline model statistic). For all other stats, "relatively" refers to the *difference* from the baseline model (i.e., the submodel statistic minus the baseline model statistic).

alpha — A number determining the (nominal) coverage 1 - alpha of the uncertainty intervals. For example, in case of a normal-approximation uncertainty interval, alpha = 2 * pnorm(-1) corresponds to a uncertainty interval stretching by one standard error on either side of the point estimate.

baseline — For summary.vsel(): Only relevant if deltas is TRUE. For plot.vsel(): Always relevant. Either "ref" or "best", indicating whether the baseline is the

reference model or the best submodel found (in terms of `stats[1]`), respectively. In case of subsampled LOO-CV, `baseline = "best"` is not supported.

`resp_oscale` Only relevant for the latent projection. A single logical value indicating whether to calculate the performance statistics on the original response scale (`TRUE`) or on latent scale (`FALSE`).

`cumulate` Passed to argument `cumulate` of `cv_proportions()`. Affects column `cv_proportions_diag` of the summary table.

`...` Arguments passed to the internal function which is used for bootstrapping (if applicable; see argument `stats`). Currently, relevant arguments are `B` (the number of bootstrap samples, defaulting to `2000`) and `seed` (see `set.seed()`, but defaulting to `NA` so that `set.seed()` is not called within that function at all).

Details

The `stats` options `"mse"`, `"rmse"`, and `"R2"` are only available for:

- the traditional projection,
- the latent projection with `resp_oscale = FALSE`,
- the latent projection with `resp_oscale = TRUE` in combination with `<refmodel>$family$cats` being `NULL`.

The `stats` option `"acc"` (= `"pctcorr"`) is only available for:

- the `binomial()` family in case of the traditional projection,
- all families in case of the augmented-data projection,
- the `binomial()` family (on the original response scale) in case of the latent projection with `resp_oscale = TRUE` in combination with `<refmodel>$family$cats` being `NULL`,
- all families (on the original response scale) in case of the latent projection with `resp_oscale = TRUE` in combination with `<refmodel>$family$cats` being not `NULL`.

The `stats` option `"auc"` is only available for:

- the `binomial()` family in case of the traditional projection,
- the `binomial()` family (on the original response scale) in case of the latent projection with `resp_oscale = TRUE` in combination with `<refmodel>$family$cats` being `NULL`.

Note that the `stats` option `"auc"` is not supported in case of subsampled LOO-CV (see argument `nloo` of `cv_varsel()`).

Value

An object of class `vselsummary`. The elements of this object are not meant to be accessed directly but instead via helper functions (`print.vselsummary()` and `performances.vselsummary()`).

See Also

`print.vselsummary()`, `performances.vselsummary()`

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Run varsel() (here without cross-validation, with L1 search, and with small
# values for `nterms_max` and `nclusters_pred`, but only for the sake of
# speed in this example; this is not recommended in general):
vs <- varsel(fit, method = "L1", nterms_max = 3, nclusters_pred = 10,
             seed = 5555)
print(summary(vs), digits = 1)
```

---

varsel *Run search and performance evaluation without cross-validation*

Description

Run the *search* part and the *evaluation* part for a projection predictive variable selection. The search part determines the predictor ranking (also known as solution path), i.e., the best submodel for each submodel size (number of predictor terms). The evaluation part determines the predictive performance of the submodels along the predictor ranking. A special method is `varsel.vsel()` which re-uses the search results from an earlier `varsel()` (or `cv_varsel()`) run, as illustrated in the main vignette.

Usage

```
varsel(object, ...)

## Default S3 method:
varsel(object, ...)

## S3 method for class 'vsel'
varsel(object, ...)

## S3 method for class 'refmodel'
varsel(
  object,
  d_test = NULL,
  method = "forward",
  ndraws = NULL,
```

```
  nclusters = 20,
  ndraws_pred = 400,
  nclusters_pred = NULL,
  refit_prj = !inherits(object, "datafit"),
  nterms_max = NULL,
  verbose = getOption("projpred.verbose", as.integer(interactive())),
  search_control = NULL,
  lambda_min_ratio = 1e-05,
  nlambda = 150,
  thresh = 1e-06,
  penalty = NULL,
  search_terms = NULL,
  search_out = NULL,
  seed = NA,
  ...
)
```

Arguments

object	An object of class refmodel (returned by get_refmodel() or init_refmodel()) or an object that can be passed to argument object of get_refmodel().
...	For varsel.default(): Arguments passed to get_refmodel() as well as to varsel.refmodel(). For varsel.vsel(): Arguments passed to varsel.refmodel(). For varsel.refmodel(): Arguments passed to the divergence minimizer (see argument div_minimizer of init_refmodel() as well as section "Draw-wise divergence minimizers" of projpred-package) when refitting the submodels for the performance evaluation (if refit_prj is TRUE).
d_test	A list of the structure outlined in section "Argument d_test" below, providing test data for evaluating the predictive performance of the submodels as well as of the reference model. If NULL, the training data is used.
method	The method for the search part. Possible options are "forward" for forward search and "L1" for L1 search. See also section "Details" below.
ndraws	Number of posterior draws used in the search part. Ignored if nclusters is not NULL or in case of L1 search (because L1 search always uses a single cluster). If both (nclusters and ndraws) are NULL, the number of posterior draws from the reference model is used for ndraws. See also section "Details" below.
nclusters	Number of clusters of posterior draws used in the search part. Ignored in case of L1 search (because L1 search always uses a single cluster). For the meaning of NULL, see argument ndraws. See also section "Details" below.
ndraws_pred	Only relevant if refit_prj is TRUE. Number of posterior draws used in the evaluation part. Ignored if nclusters_pred is not NULL. If both (nclusters_pred and ndraws_pred) are NULL, the number of posterior draws from the reference model is used for ndraws_pred. See also section "Details" below.
nclusters_pred	Only relevant if refit_prj is TRUE. Number of clusters of posterior draws used in the evaluation part. For the meaning of NULL, see argument ndraws_pred. See also section "Details" below.

refit_prj
: For the evaluation part, should the projections onto the submodels along the predictor ranking be performed again using ndraws_pred draws or nclusters_pred clusters (TRUE) or should their projections from the search part, which used ndraws draws or nclusters clusters, be re-used (FALSE)?

nterms_max
: Maximum submodel size (number of predictor terms) up to which the search is continued. If NULL, then min(19, D) is used where D is the number of terms in the reference model (or in search_terms, if supplied). Note that nterms_max does not count the intercept, so use nterms_max = 0 for the intercept-only model. (Correspondingly, D above does not count the intercept.)

verbose
: A single integer value from the set $\{0, 1, 2, 3, 4\}$ (for varsel(), 3 and 4 have the same effect), indicating how much information (if any) to print out during the computations. Higher values indicate that more information should be printed, 0 deactivates the verbose mode. Internally, argument verbose is coerced to integer via as.integer(), so technically, a single logical value or a single numeric value work as well.

search_control
: A list of "control" arguments (i.e., tuning parameters) for the search. In case of forward search, these arguments are passed to the divergence minimizer (see argument div_minimizer of init_refmodel() as well as section "Draw-wise divergence minimizers" of projpred-package). In case of forward search, NULL causes ... to be used not only for the performance evaluation, but also for the search. In case of L1 search, possible arguments are:

  - lambda_min_ratio: Ratio between the smallest and largest lambda in the L1-penalized search (default: 1e-5). This parameter essentially determines how long the search is carried out, i.e., how large submodels are explored. No need to change this unless the program gives a warning about this.
  - nlambda: Number of values in the lambda grid for L1-penalized search (default: 150). No need to change this unless the program gives a warning about this.
  - thresh: Convergence threshold when computing the L1 path (default: 1e-6). Usually, there is no need to change this.

lambda_min_ratio
: Deprecated (please use search_control instead). Only relevant for L1 search. Ratio between the smallest and largest lambda in the L1-penalized search. This parameter essentially determines how long the search is carried out, i.e., how large submodels are explored. No need to change this unless the program gives a warning about this.

nlambda
: Deprecated (please use search_control instead). Only relevant for L1 search. Number of values in the lambda grid for L1-penalized search. No need to change this unless the program gives a warning about this.

thresh
: Deprecated (please use search_control instead). Only relevant for L1 search. Convergence threshold when computing the L1 path. Usually, there is no need to change this.

penalty
: Only relevant for L1 search. A numeric vector determining the relative penalties or costs for the predictors. A value of 0 means that those predictors have no cost and will therefore be selected first, whereas Inf means those predictors will never be selected. If NULL, then 1 is used for each predictor.

search_terms — Only relevant for forward search. A custom character vector of predictor term blocks to consider for the search. Section "Details" below describes more precisely what "predictor term block" means. The intercept ("1") is always included internally via union(), so there's no difference between including it explicitly or omitting it. The default search_terms considers all the terms in the reference model's formula.

search_out — Intended for internal use.

seed — Pseudorandom number generation (PRNG) seed by which the same results can be obtained again if needed. Passed to argument seed of set.seed(), but can also be NA to not call set.seed() at all. If not NA, then the PRNG state is reset (to the state before calling varsel()) upon exiting varsel(). Here, seed is used for clustering the reference model's posterior draws (if !is.null(nclusters) or !is.null(nclusters_pred)) and for drawing new group-level effects when predicting from a multilevel submodel (however, not yet in case of a GAMM).

Details

Arguments ndraws, nclusters, nclusters_pred, and ndraws_pred are automatically truncated at the number of posterior draws in the reference model (which is 1 for datafits). Using less draws or clusters in ndraws, nclusters, nclusters_pred, or ndraws_pred than posterior draws in the reference model may result in slightly inaccurate projection performance. Increasing these arguments affects the computation time linearly.

For argument method, there are some restrictions: For a reference model with multilevel or additive formula terms or a reference model set up for the augmented-data projection, only the forward search is available. Furthermore, argument search_terms requires a forward search to take effect.

L1 search is faster than forward search, but forward search may be more accurate. Furthermore, forward search may find a sparser model with comparable performance to that found by L1 search, but it may also overfit when more predictors are added. This overfit can be detected by running search validation (see cv_varsel()).

An L1 search may select an interaction term before all involved lower-order interaction terms (including main-effect terms) have been selected. In **projpred** versions > 2.6.0, the resulting predictor ranking is automatically modified so that the lower-order interaction terms come before this interaction term, but if this is conceptually undesired, choose the forward search instead.

The elements of the search_terms character vector don't need to be individual predictor terms. Instead, they can be building blocks consisting of several predictor terms connected by the + symbol. To understand how these building blocks work, it is important to know how **projpred**'s forward search works: It starts with an empty vector chosen which will later contain already selected predictor terms. Then, the search iterates over model sizes $j \in \{0, ..., J\}$ (with J denoting the maximum submodel size, not counting the intercept). The candidate models at model size j are constructed from those elements from search_terms which yield model size j when combined with the chosen predictor terms. Note that sometimes, there may be no candidate models for model size j. Also note that internally, search_terms is expanded to include the intercept ("1"), so the first step of the search (model size 0) always consists of the intercept-only model as the only candidate.

As a search_terms example, consider a reference model with formula y ~ x1 + x2 + x3. Then, to ensure that x1 is always included in the candidate models, specify search_terms = c("x1", "x1 + x2", "x1 + x3", "x1 + x2 + x3") (or, in a simpler way that leads to the same results, search_terms = c("x1", "x1 + x2", "x1 + x3"), for which helper function force_search_terms() exists). This

search would start with y ~ 1 as the only candidate at model size 0. At model size 1, y ~ x1 would be the only candidate. At model size 2, y ~ x1 + x2 and y ~ x1 + x3 would be the two candidates. At the last model size of 3, y ~ x1 + x2 + x3 would be the only candidate. As another example, to exclude x1 from the search, specify search_terms = c("x2", "x3", "x2 + x3") (or, in a simpler way that leads to the same results, search_terms = c("x2", "x3")).

Value

An object of class vsel. The elements of this object are not meant to be accessed directly but instead via helper functions (see the main vignette and projpred-package).

Argument d_test

If not NULL, then d_test needs to be a list with the following elements:

- data: a data.frame containing the predictor variables for the test set. In case of the latent projection, this data.frame is also used for evaluating attribute cens_var of the latent_ll_oscale function, so if cens_var is not NULL, data also needs to contain the data for the variable from cens_var.
- offset: a numeric vector containing the offset values for the test set (if there is no offset, use a vector of zeros).
- weights: a numeric vector containing the observation weights for the test set (if there are no observation weights, use a vector of ones).
- y: a vector or a factor containing the response values for the test set. In case of the latent projection, this has to be a vector containing the *latent* response values, but it can also be a vector full of NAs if latent-scale post-processing is not needed.
- y_oscale: Only needs to be provided in case of the latent projection where this needs to be a vector or a factor containing the *original* (i.e., non-latent) response values for the test set.

See Also

cv_varsel()

Examples

```
# Data:
dat_gauss <- data.frame(y = df_gaussian$y, df_gaussian$x)

# The `stanreg` fit which will be used as the reference model (with small
# values for `chains` and `iter`, but only for technical reasons in this
# example; this is not recommended in general):
fit <- rstanarm::stan_glm(
  y ~ X1 + X2 + X3 + X4 + X5, family = gaussian(), data = dat_gauss,
  QR = TRUE, chains = 2, iter = 500, refresh = 0, seed = 9876
)

# Run varsel() (here without cross-validation, with L1 search, and with small
# values for `nterms_max` and `nclusters_pred`, but only for the sake of
# speed in this example; this is not recommended in general):
vs <- varsel(fit, method = "L1", nterms_max = 3, nclusters_pred = 10,
```

```
            seed = 5555)
# Now see, for example, `?print.vsel`, `?plot.vsel`, `?suggest_size.vsel`,
# and `?ranking` for possible post-processing functions.
```

`y_wobs_offs` *Extract response values, observation weights, and offsets*

Description

A helper function for extracting response values, observation weights, and offsets from a dataset. It is designed for use in the `extract_model_data` function of custom reference model objects (see `init_refmodel()`).

Usage

```
y_wobs_offs(newdata, wrhs = NULL, orhs = NULL, resp_form)
```

Arguments

`newdata`	The `data.frame` from which at least the response values should be extracted.
`wrhs`	Either a right-hand side formula consisting only of the variable in `newdata` containing the weights, `NULL` (for using a vector of ones), or directly the numeric vector of observation weights.
`orhs`	Either a right-hand side formula consisting only of the variable in `newdata` containing the offsets, `NULL` (for using a vector of zeros), or directly the numeric vector of offsets.
`resp_form`	If this is a formula, then the second element of this formula (if the formula is a standard formula with both left-hand and right-hand side, then its second element is the left-hand side; if the formula is a right-hand side formula, then its second element is the right-hand side) will be extracted from `newdata` (so `resp_form` may be either a standard formula or a right-hand side formula, but in the latter case, the right-hand side should consist only of the response variable). In all other cases, `NULL` will be returned for element `y` of the output `list`.

Value

A `list` with elements `y`, `weights`, and `offset`, each being a numeric vector containing the data for the response, the observation weights, and the offsets, respectively. An exception is that `y` may also be `NULL` (depending on argument `resp_form`), a non-numeric vector, or a `factor`.

See Also

`init_refmodel()`

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